

# NASA Advanced Modeling and Simulation Seminar

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## UQ Analysis of DNS data with RANS-DNS simulations



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In collaboration with

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NASA Ames

NASA NNX12AJ61A

# My background



## Education

Ph. D. **Fluid & Plasma Mechanics**

M. S. **Physics**, Focus area: **Aerophysics & Gas Dynamics**

## Affiliations

2010 - present	<b>University of New Mexico:</b> Mechanical Engineering
2003 - 2010	<b>Florida State University:</b> School of Computational Science Center for Advanced Power
2001 - 2003	<b>Texas A&amp;M University:</b> Aerospace Engineering
1999 - 2001	<b>Stanford University:</b> Center for Turbulence Research
1996 - 1999	<b>Institute of Theoretical &amp; Applied Mechanics</b> , Russia
1989 - 1993	<b>Institute of Thermophysics</b> , Russia

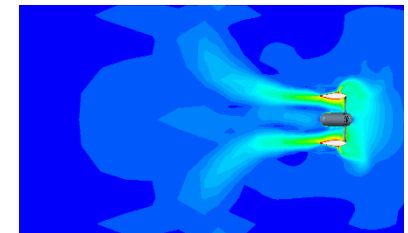
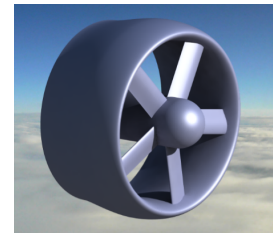
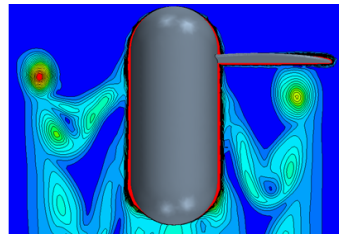
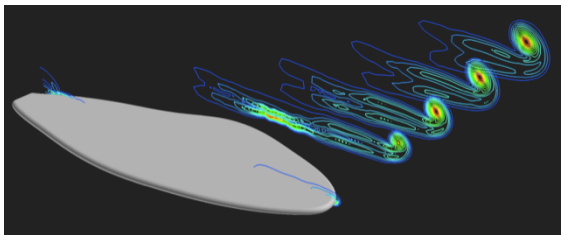
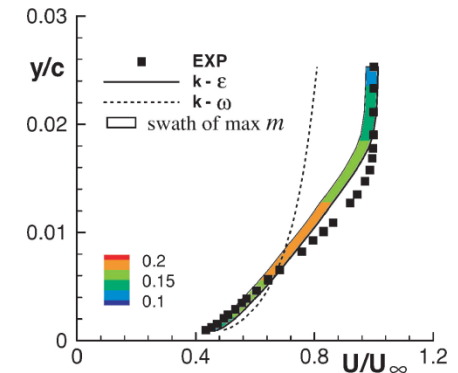
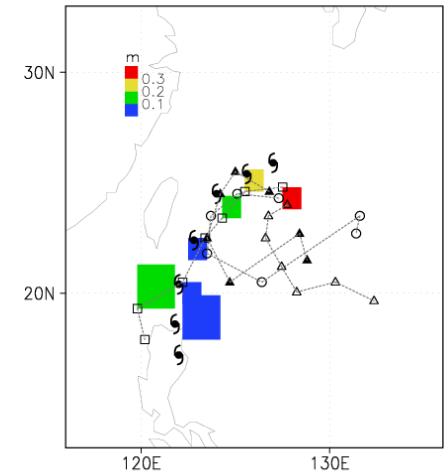
## Research Interests

- Turbulence modeling for aerodynamic flows: [statistical closures](#), DNS
- Analysis of simulation uncertainty:  
[RANS-DNS simulations](#), [evidence theory-based multi-model predictions](#)
- Biomimetic rotor design for small rotorcrafts
- Alternative wind energy harvesting
- Survivability of networks

# My background

## Research Areas

- **Turbulence modeling:** RANS, DNS
- **Analysis of simulation uncertainty:** RANS-DNS simulations, evidence theory
- **Multi-model predictions** evidence theory
- **Rotor design for small rotorcrafts**
- **Non-rotary wind energy harvesting**
- **Survivability of networks:** analysis and biomimetic design for power systems



# Motivation

- **Turbulence modeling: RANS**

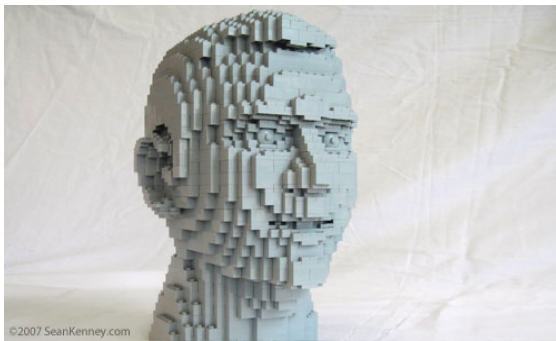
**NNX12AJ61A goal:**

to develop an accurate physics-based general framework capable of accurate modeling a wide range of aerodynamic turbulent flows without wall functions and with a minimum number of unknown coefficients

**Possible solution:** Fourth-order RANS (FORANS) closures

# Justification

- The turbulent flow field representation by statistical moments is equivalent to the PDF representation.
- There is a direct connection between the number of equations solved and the amount of physics involved.
- Assumptions about PDF can be introduced in  $> 3^{\text{rd}}$ -order closures.
- A FORANS model can possibly be reduced to a simpler model without wall-functions and unknown coefficients.



[http://www.seankenney.com/portfolio/the\\_accomplished\\_man/](http://www.seankenney.com/portfolio/the_accomplished_man/)



(Photo: jeshko) Youtube/jeshko

# FORANS closures

$$\frac{\bar{D}U_i}{Dt} = - \frac{\partial \langle u_i u_j \rangle}{\partial x_j} + \dots$$

Standard models

$$\frac{\bar{D} \langle u_i u_j \rangle}{Dt} = - \frac{\partial \langle u_i u_j u_k \rangle}{\partial x_k} + \Pi_{ij} - \epsilon_{ij} + \dots$$

$$\frac{\bar{D} \langle u_i u_j u_k \rangle}{Dt} = - \frac{\partial \langle u_i u_j u_k u_l \rangle}{\partial x_l} + \Pi_{ijk} - \epsilon_{ijk} + \dots$$

$$\frac{\bar{D} \langle u_i u_j u_k u_l \rangle}{Dt} = - \frac{\partial \langle u_i u_j u_k u_l u_m \rangle}{\partial x_m} + \Pi_{ijkl} - \epsilon_{ijkl} + \dots$$

FORANS



Turbulent diffusion

Truncated Gram-Charlier series expansions



Velocity-pressure gradient correlations

Data-driven model



Dissipation

DNS data

# Truncated Gram-Charlier series expansions:

$$\langle u^5 \rangle = 10 \langle u^2 \rangle \langle u^3 \rangle$$

Kampé de Fériet (1966)  
Durst et al. (BL, 1992)

$$\langle v^5 \rangle = 10 \langle v^2 \rangle \langle v^3 \rangle$$

$$\langle u^4 v \rangle = 6 \langle u^2 \rangle \langle u^2 v \rangle + 4 \langle u^3 \rangle \langle uv \rangle$$

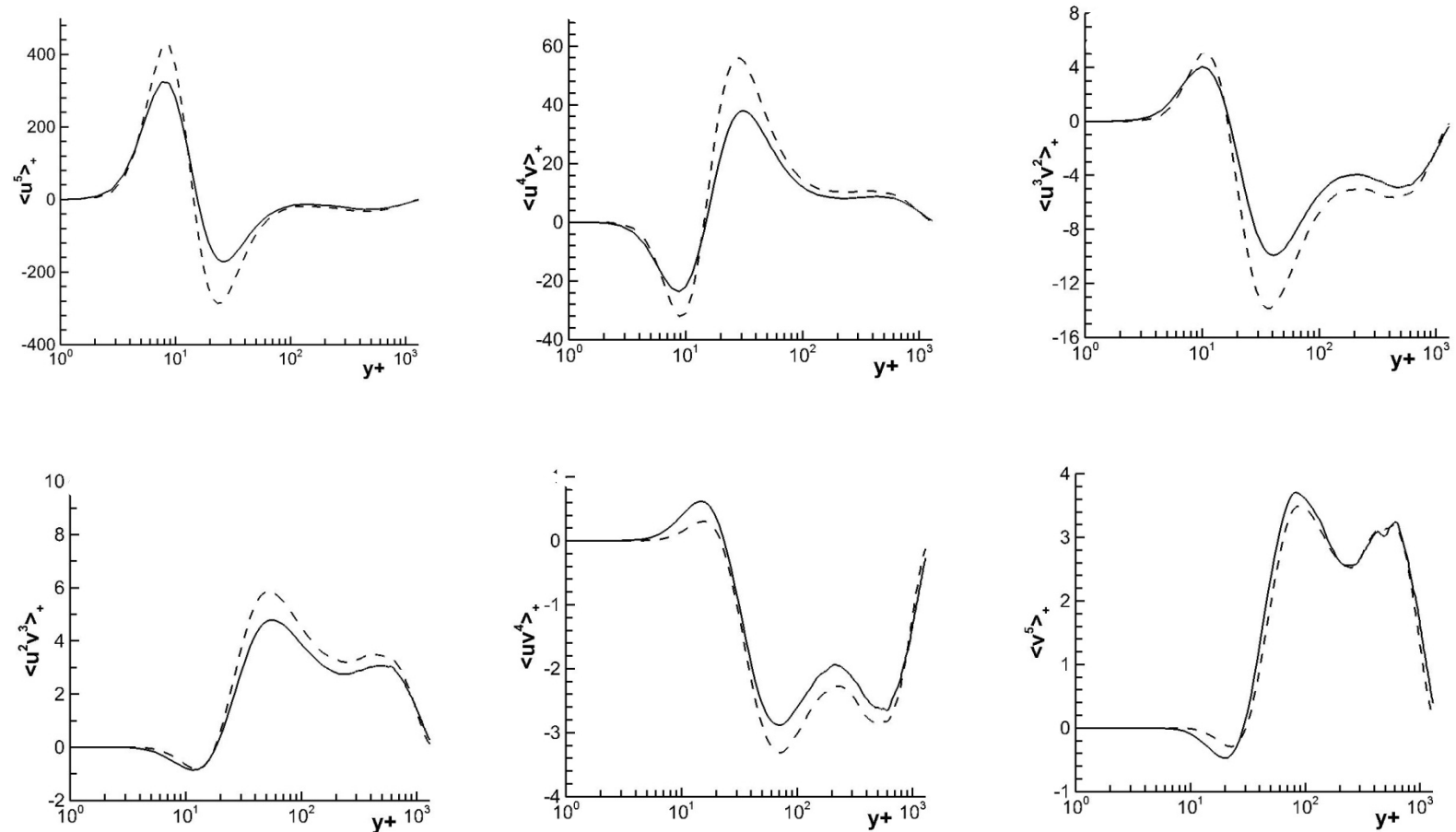
$$\langle uv^4 \rangle = 6 \langle v^2 \rangle \langle uv^2 \rangle + 4 \langle v^3 \rangle \langle uv \rangle$$

$$\langle u^2 v^3 \rangle = 6 \langle uv \rangle \langle uv^2 \rangle + \langle u^2 \rangle \langle v^3 \rangle + 3 \langle u^2 v \rangle \langle v^2 \rangle$$

$$\langle u^3 v^2 \rangle = 6 \langle uv \rangle \langle u^2 v \rangle + \langle u^3 \rangle \langle v^2 \rangle + 3 \langle uv^2 \rangle \langle u^2 \rangle$$

# Validation results: ZPG BL

$Re_\theta = 4101, 5200$

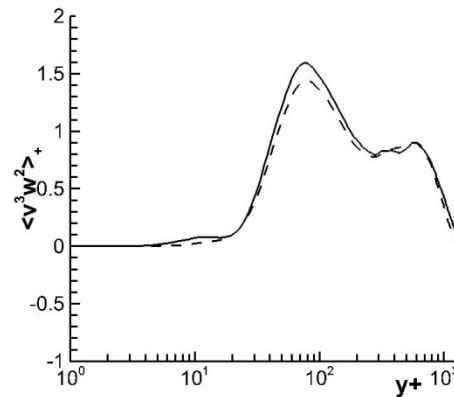
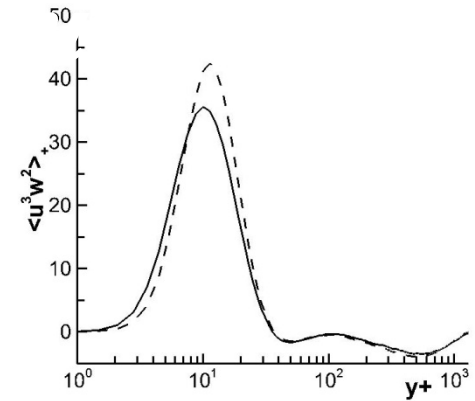
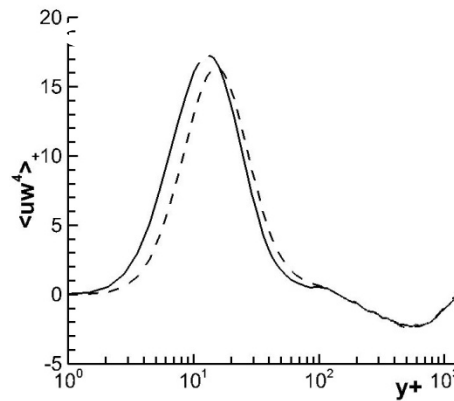
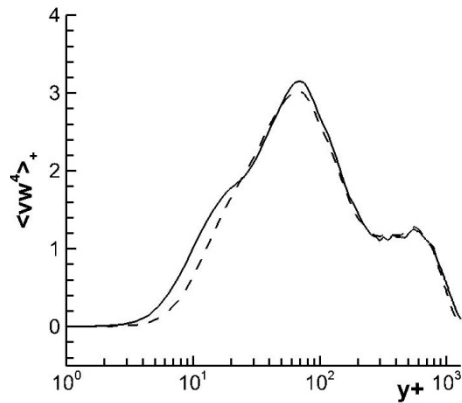


— DNS      - - - Gram-Charlier representation using DNS data



# DNS validation: ZPG BL

— DNS      - - - Gram-Charlier using DNS data

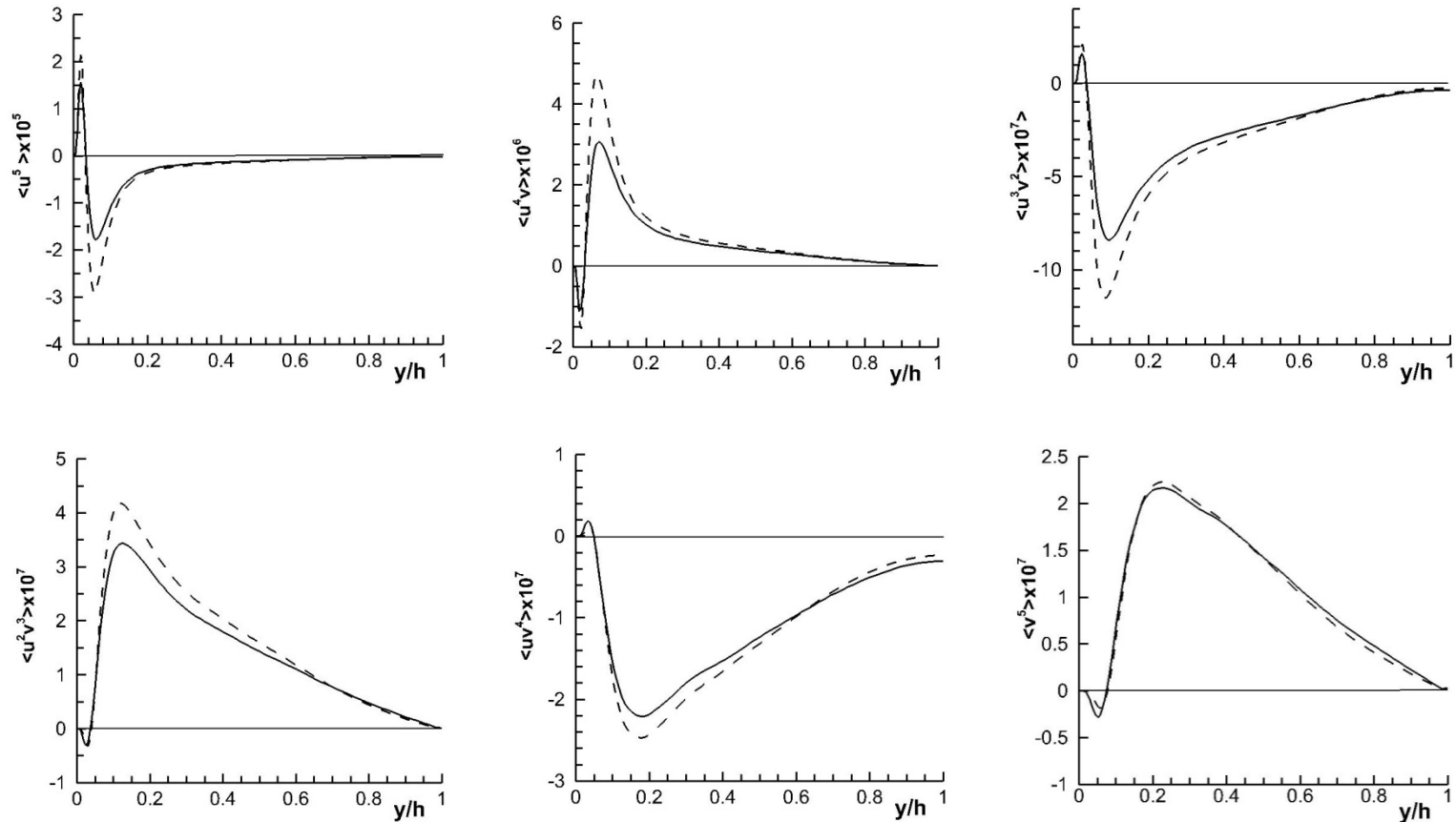


Poroseva et al., Int. J. Heat Fluid Flow, 2015

# DNS validation: channel flow

$Re_\tau = 392$

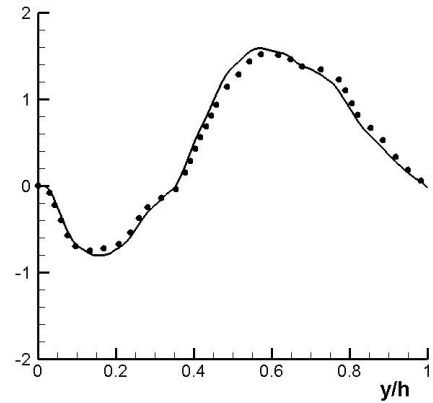
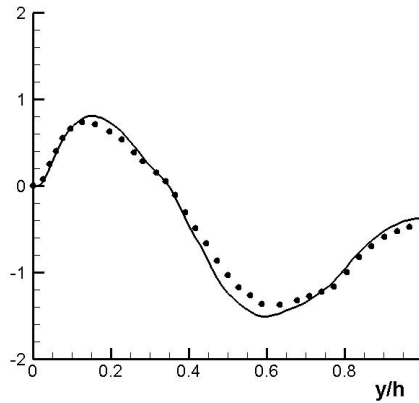
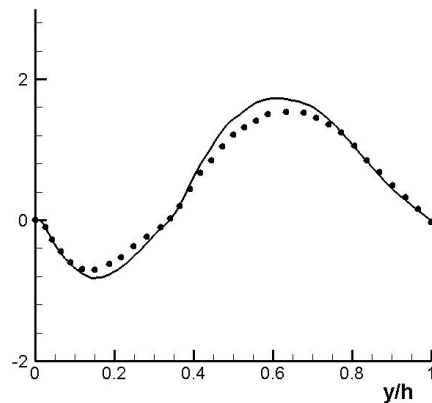
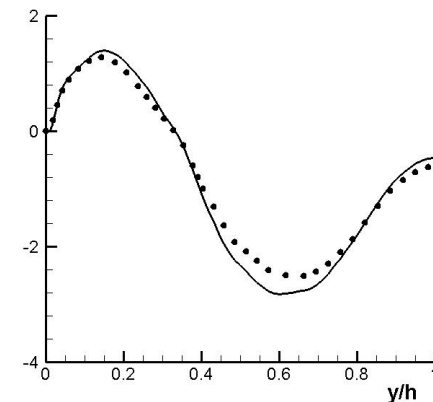
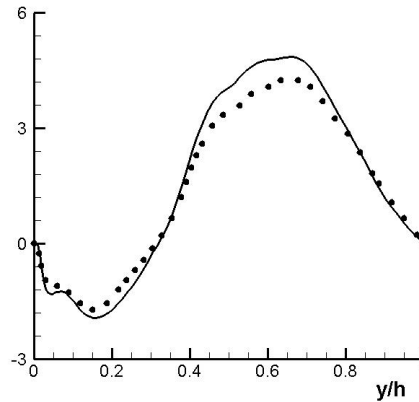
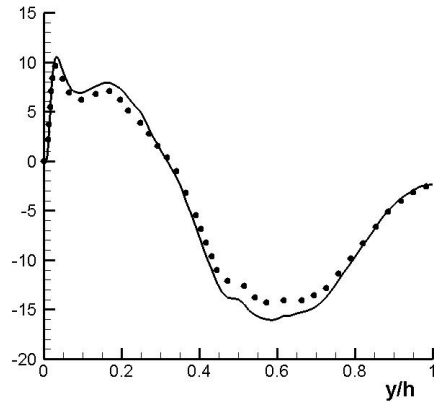
— DNS      - - - Gram-Charlier using DNS data



[http://turbmodels.larc.nasa.gov/Other\\_DNS\\_Data/high-order-channel.html](http://turbmodels.larc.nasa.gov/Other_DNS_Data/high-order-channel.html)

# Strained Channel:

$$A_{22}t = 0.772$$



... DNS      — Gram-Charlier representation using DNS data

[http://turbmodels.larc.nasa.gov/Other\\_DNS\\_Data/high-order-channel.html](http://turbmodels.larc.nasa.gov/Other_DNS_Data/high-order-channel.html)

# Data-driven velocity/pressure-gradient models (planar flows, v.2)

$$\Pi_{xy} = -0.92D_{xy}^T - 0.92P_{xy} - 0.3D_{xy}^M$$

$$\Pi_{xx} = -0.78\Pi_{xy} - 0.7\Pi_{yy} - 0.25D_{xy}^T + 0.01D_{xx}^M$$

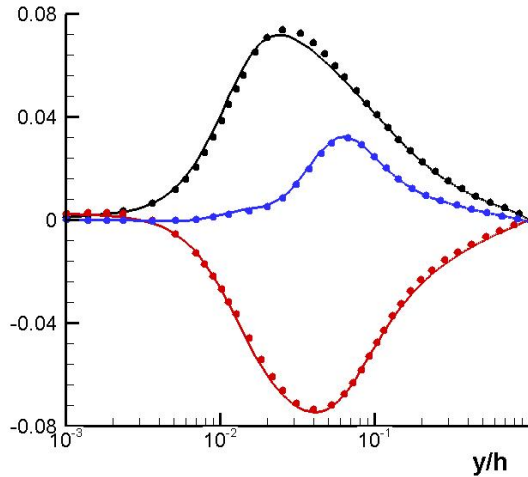
$$\Pi_{yy} = -0.45P_{xy} - 0.031P_{xx} - 1.35D_{yy}^T + 1.15D_{zz}^T - 0.47D_{xy}^T + 0.2D_{yy}^M$$

Poroseva et al., AIAA2015-3067

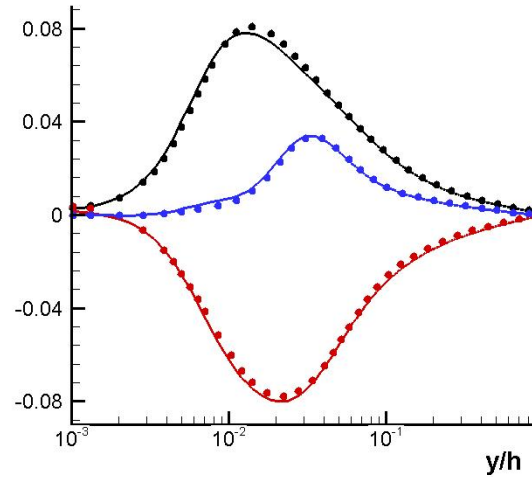
Poroseva & Murman, Proc. TSFP-9, TSFP-10

# Fully-developed channel

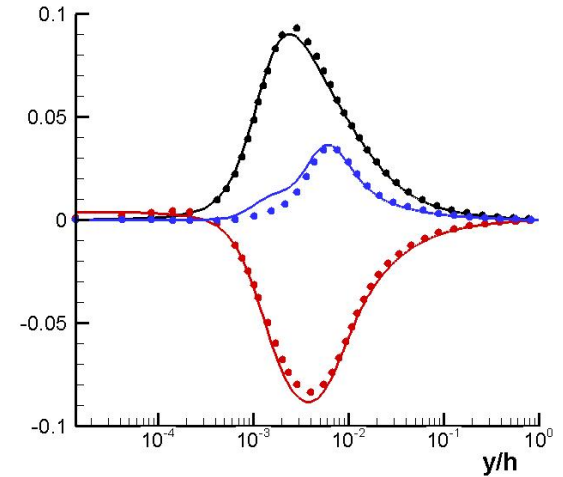
**$Re_T = 550$**



**$Re_T = 1000$**

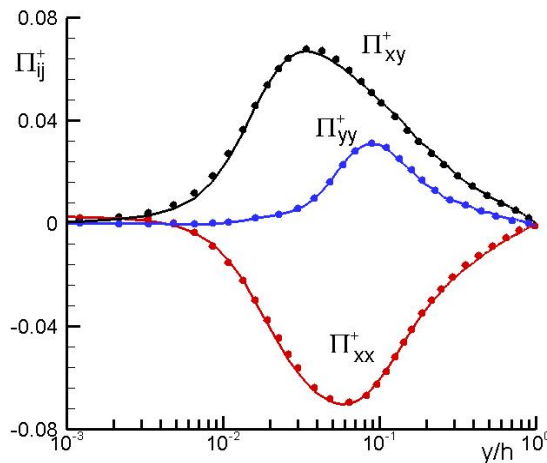


**$Re_T = 5200$**



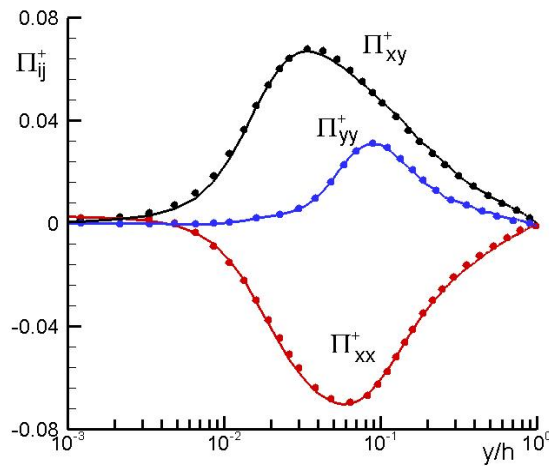
Lee & Moser, JFM, 2015

**$Re_T = 395$**

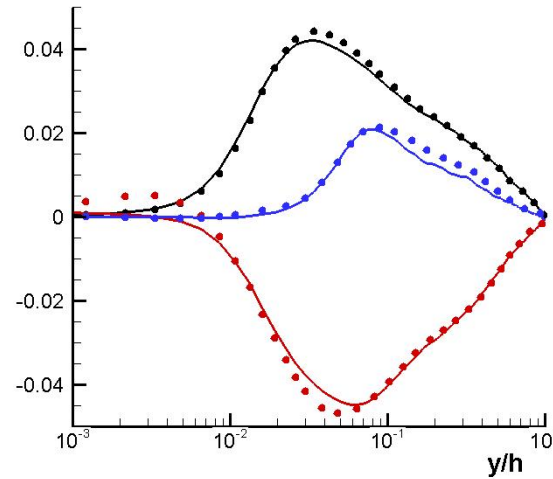


Jeyapaul et al., AIAA2014-2088

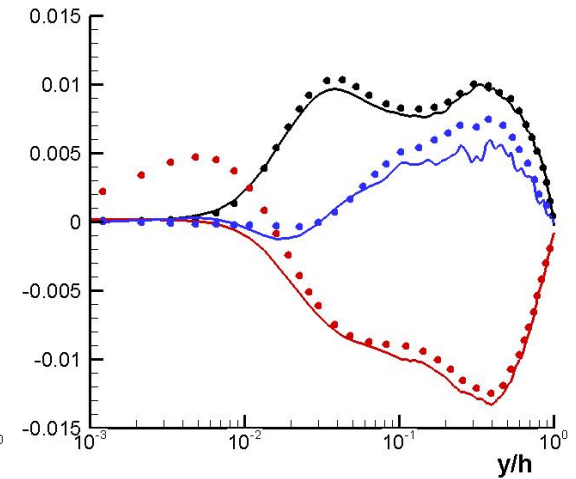
# Strained channel/ZPG BL



$A_{22}t = 0$



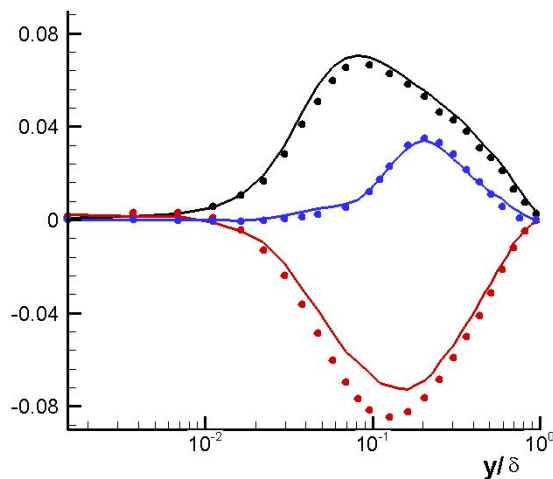
$A_{22}t = 0.281$



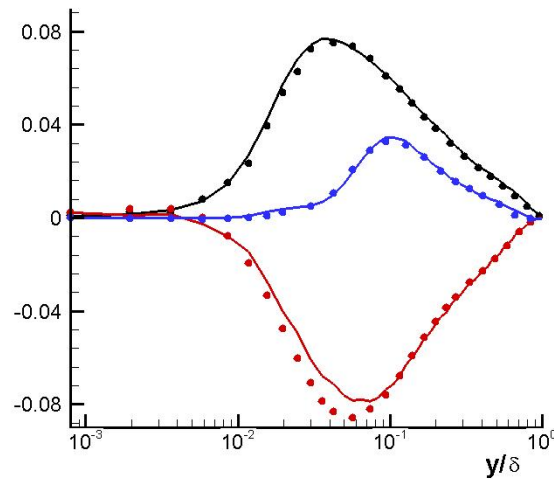
$A_{22}t = 0.772$

[http://turbmodels.larc.nasa.gov/Other\\_DNS\\_Data/high-order-channel.html](http://turbmodels.larc.nasa.gov/Other_DNS_Data/high-order-channel.html)

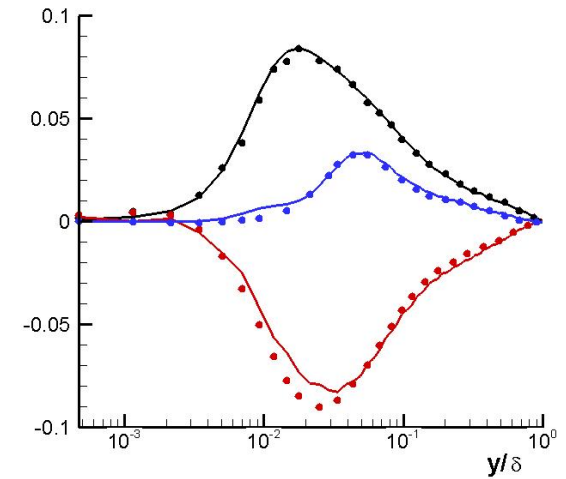
**$Re_\tau = 300$**



**$Re_\tau = 670$**



**$Re_\tau = 1410$**

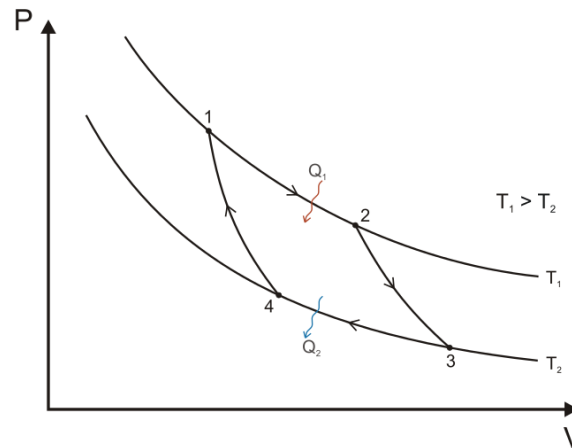


Spalart, JFM, 1988

**Why cannot one obtain the accurate solution of the RANS equations with very accurate models for their terms?**

**What is the limit for physics-based RANS models?**

**Because we cannot have 100% efficient engine...sort of...**



# “Ideal” RANS model

$$\frac{\bar{D} \langle u_i u_j u_k u_l \rangle}{Dt} = D_{ijkl}^M + D_{ijkl}^T + P_{ijkl} + P_{ijkl}^T + \Pi_{ijkl} - \varepsilon_{ijkl}$$

$$\frac{\bar{D} \langle u_i u_j u_k \rangle}{Dt} = D_{ijk}^M + D_{ijk}^T + P_{ijk} + P_{ijk}^T + \Pi_{ijk} - \varepsilon_{ijk}$$

$$\frac{\bar{D} \langle u_i u_j \rangle}{Dt} = D_{ij}^M + D_{ij}^T + P_{ij} + \Pi_{ij} - \varepsilon_{ij}$$

$$\frac{\bar{D} U_i}{Dt} = \nu \frac{\partial^2 U_i}{\partial x_j \partial x_j} - \frac{1}{\rho} \frac{\partial P}{\partial x_i} - \frac{\partial \langle u_i u_j \rangle}{\partial x_j}$$

 Data from direct numerical simulations

**This is the definition of RANS-DNS simulations**



- Framework should be applicable to any flow simulations
- A type of differential equations should be preserved
- A same solver should be used as in simulations with a model

Poroseva et al., AIAA2015-3067

Poroseva & Murman, Proc. TSFP-9, 2015

# Numerical procedure

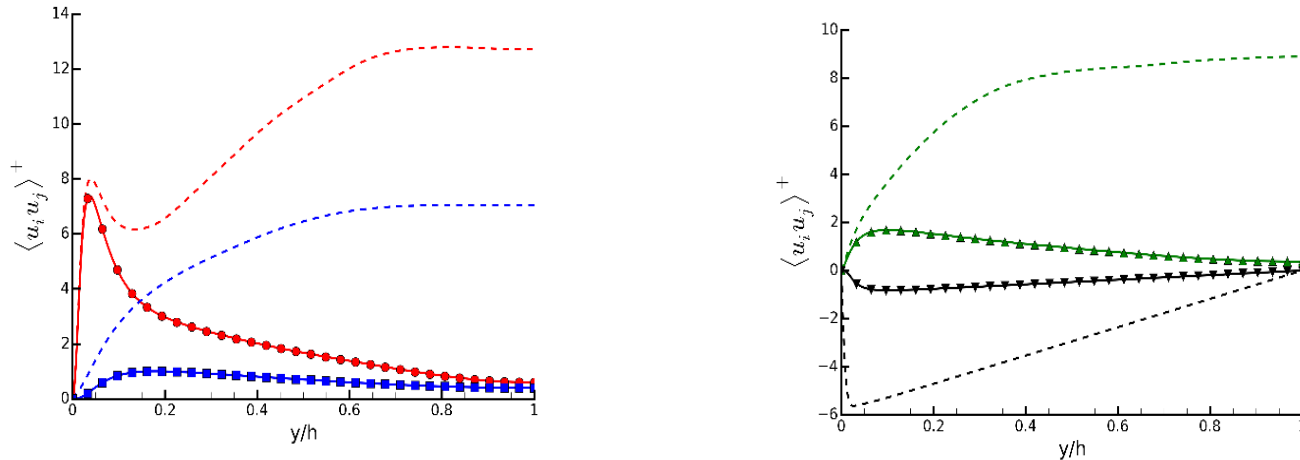
## Test flows:

- a fully-developed channel flow at the DNS flow conditions  
Lee & Moser, 2015  
Jeyapaul et al. 2015
- zero-pressure gradient boundary layer over a flat plate  
Sillero et al., 2013

**Solvers:** OpenFOAM and in-house code for fully-developed flows

**Grids:** from DNS + grid sensitivity analysis

# “Ideal” model (RANS-DNS) results



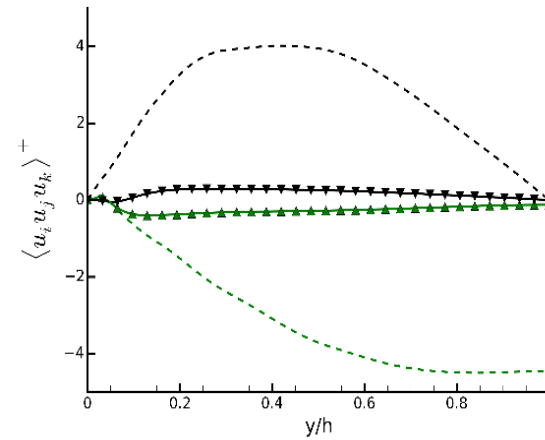
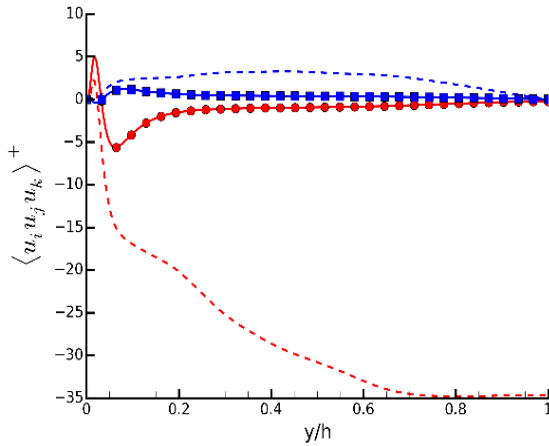
DNS data:  $\bullet$   $\langle u^2 \rangle$ ,  $\blacksquare$   $\langle v^2 \rangle$ ,  $\blacktriangle$   $\langle w^2 \rangle$ ,  $\blacktriangledown$   $\langle uv \rangle$ , RANS-DNS - - -  
Jeyapaul et al. 2015

**$\text{Re}_\tau = 395$**

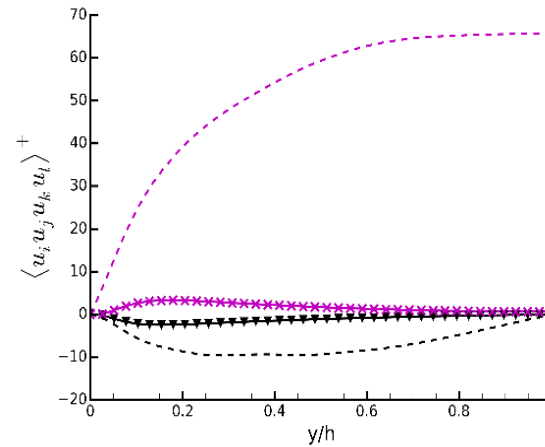
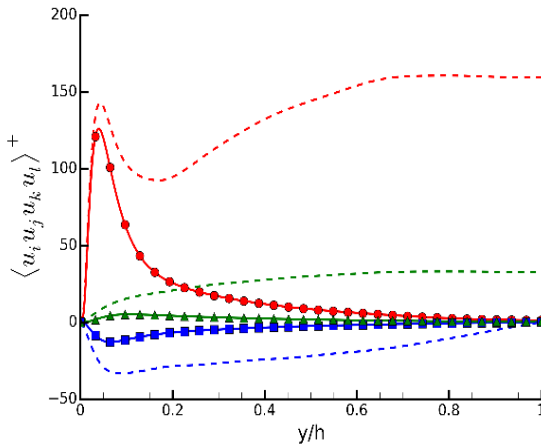
Symbols: DNS data

Dashed lines: RANS-DNS simulations

# RANS-DNS results



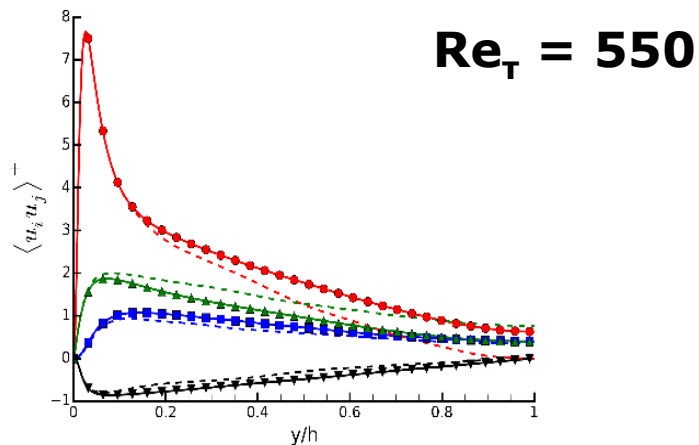
DNS data:  $\bullet <u^3>$ ,  $\blacksquare <u^2 v>$ ,  $\blacktriangle <uv^2>$ ,  $\blacktriangledown <v^3>$ , RANS-DNS - - -



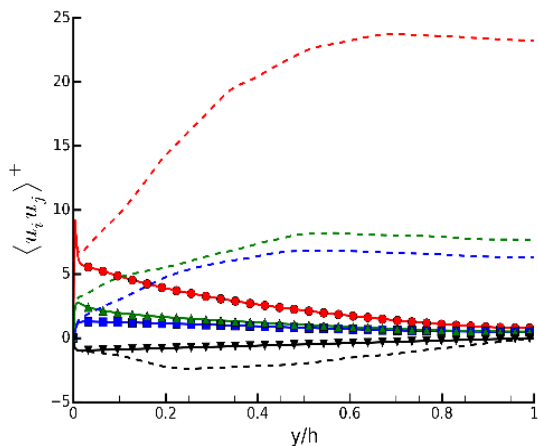
DNS data:  $\bullet <u^4>$ ,  $\blacksquare <u^3 v>$ ,  $\blacktriangle <u^2 v^2>$ ,  $\blacktriangledown <uv^3>$ ,  $\times <v^4>$ , RANS-DNS - - -

# RANS-DNS results

Similar results were obtained with different database  
(Lee & Moser, JFM, 2015)



and at different Reynolds number:  $Re_T = 5200$



DNS data:  $\bullet <u^2>$ ,  $\blacksquare <v^2>$ ,  $\blacktriangle <w^2>$ ,  $\blacktriangledown <uv>$ , RANS-DNS - - -

# Uncertainty analysis

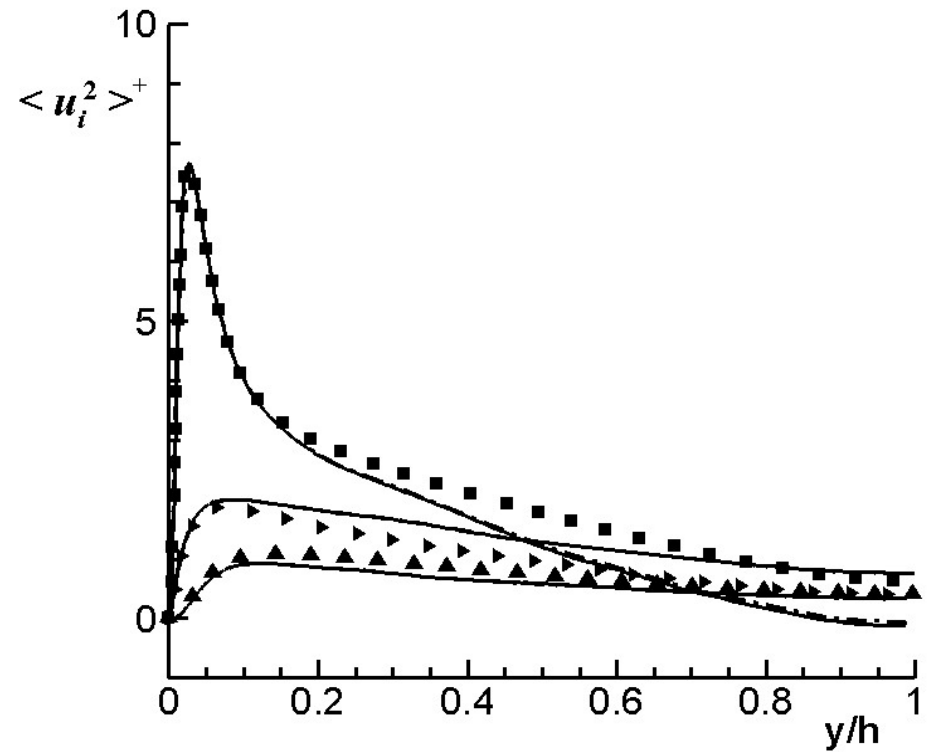
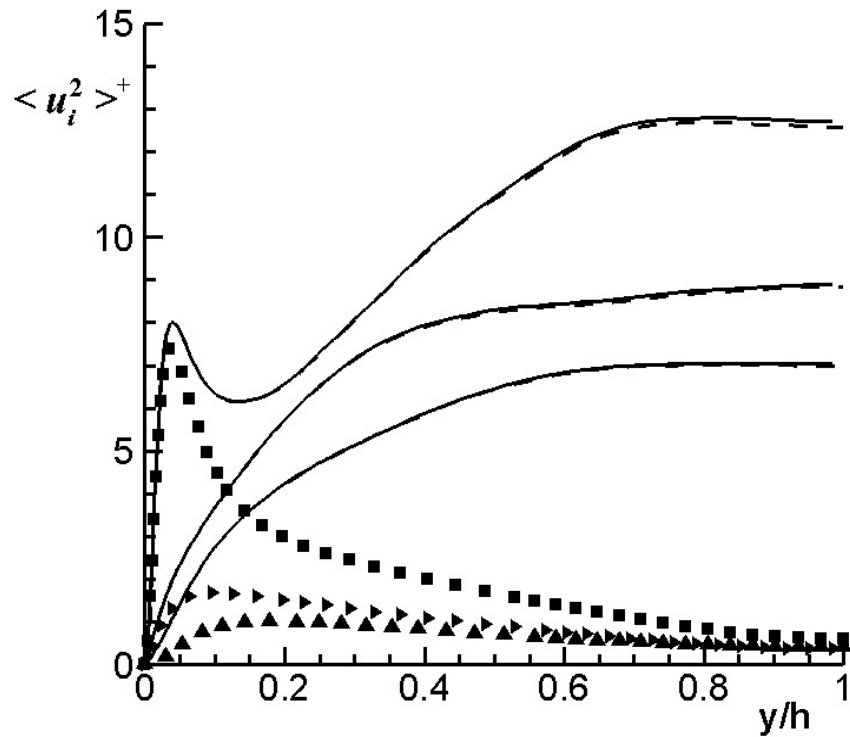
**Solutions of the “ideal” model with no modeling involved are unphysical....**

**One cannot expect a physics-based turbulence model to outperform the solution based on DNS data....**

## **Uncertainty sources in RANS-DNS simulations**

- Numerical procedure used in RANS simulations
- DNS data
- Interaction of both

# UQ analysis of RANS-DNS simulations



$Re_\tau = 550$

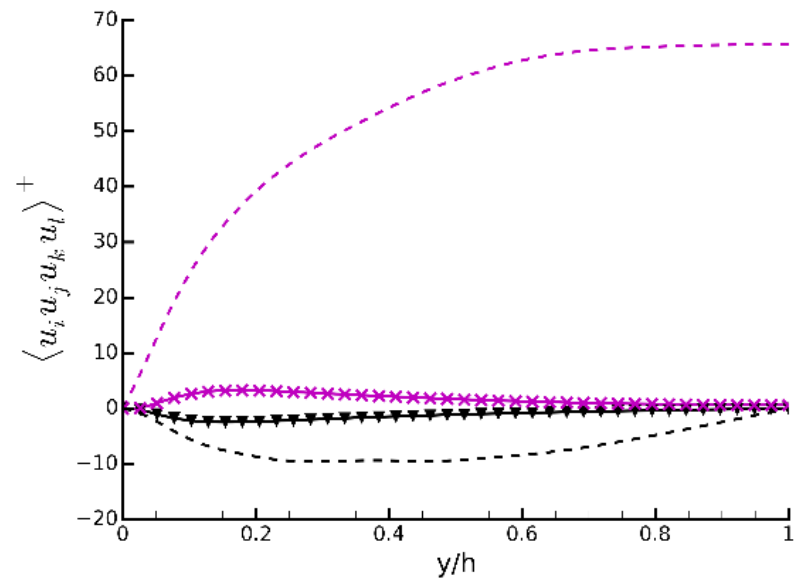
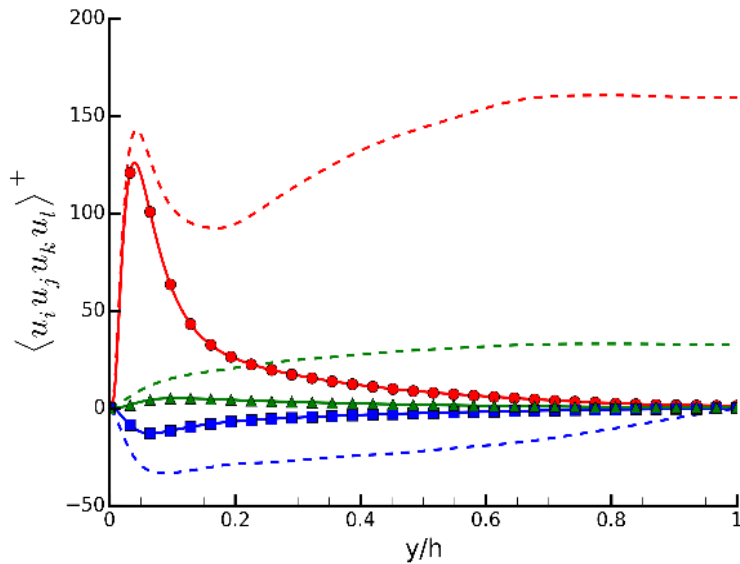
**Different solvers**

**Different grids**

Poroseva et al., Physics of Fluids, 2016

# UQ analysis of RANS-DNS simulations

And this is due to inaccuracies of DNS data



$$0 = D_{ij}^M + D_{ij}^T + P_{ij} + \Pi_{ij} - \varepsilon_{ij}$$

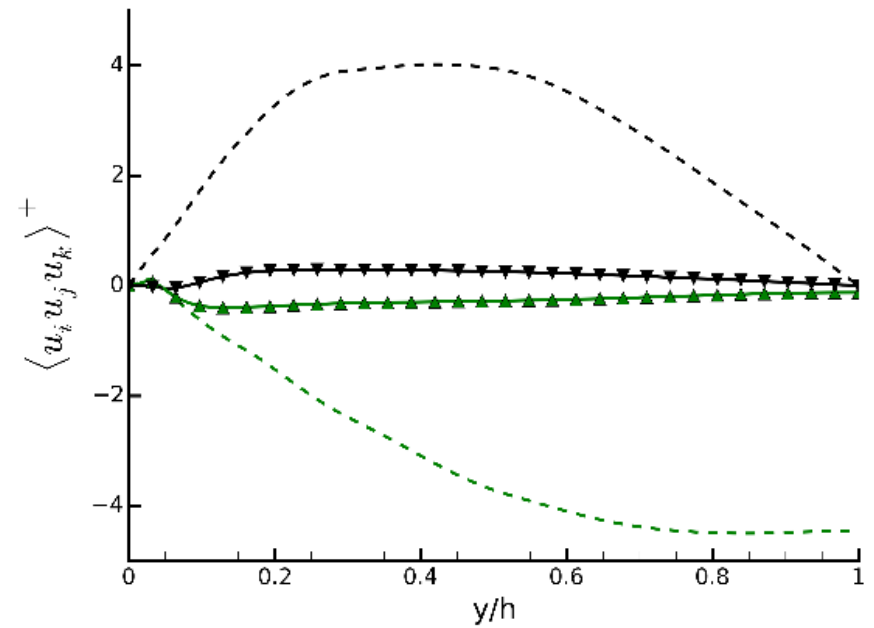
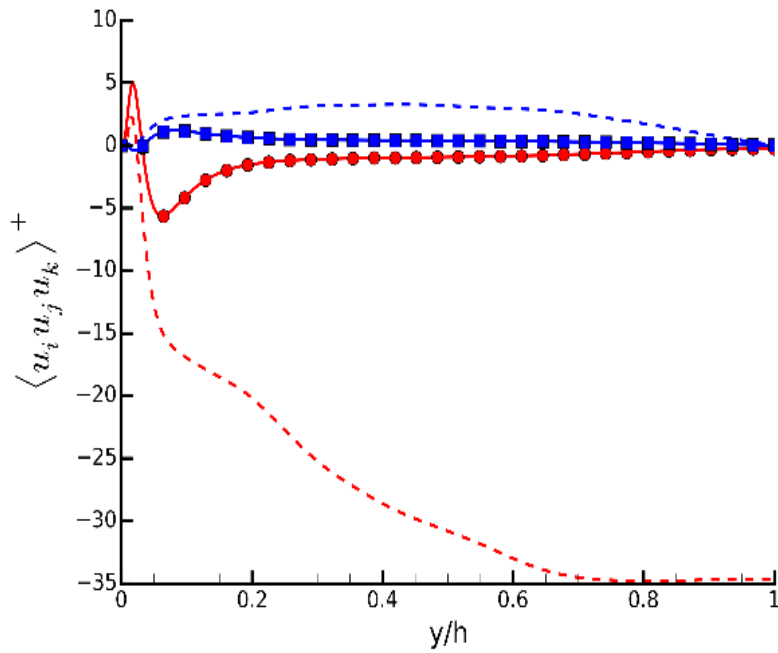
Dashed lines

$$0 = D_{ij}^M + D_{ij}^T + P_{ij} + \Pi_{ij} - \varepsilon_{ij} - \text{Err}_{ij}$$

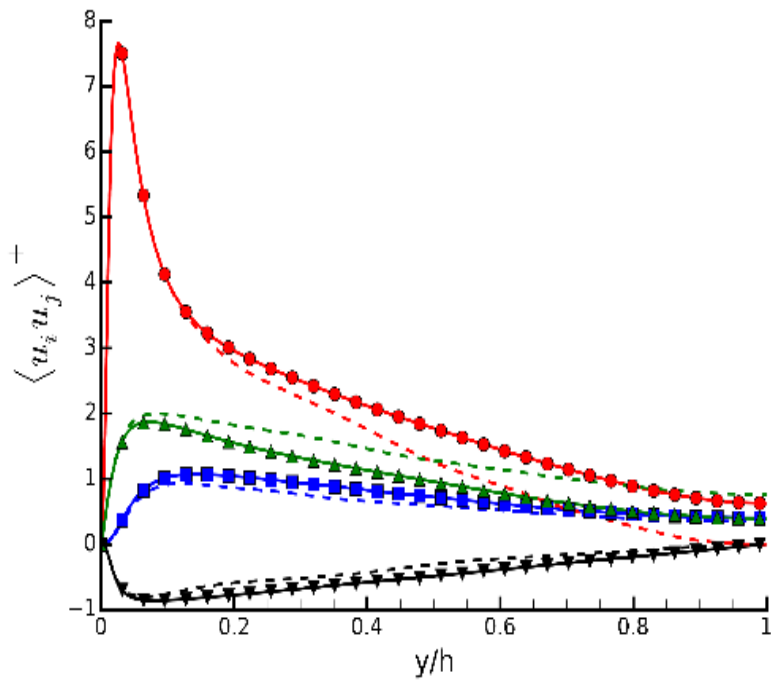
Solid lines



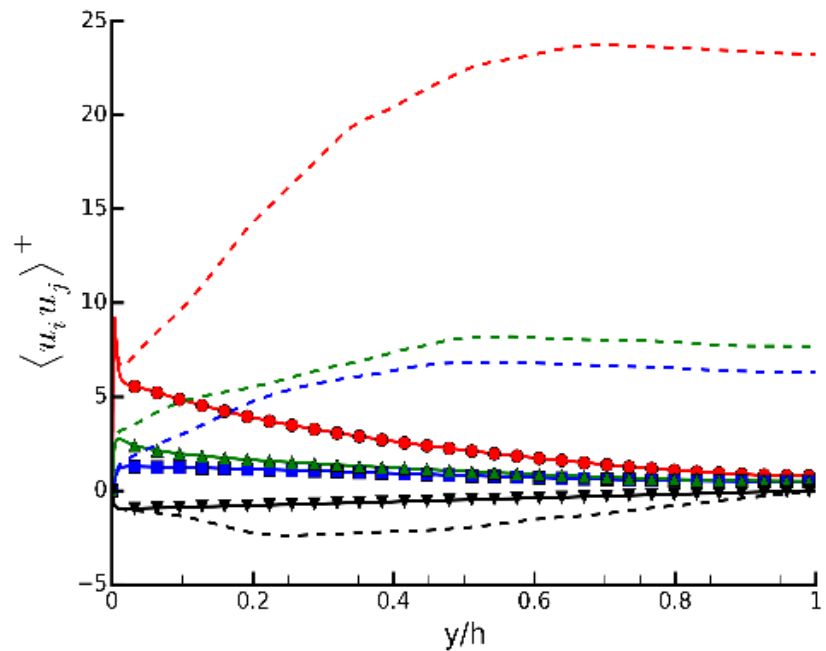
**$Re_\tau = 395$**



DNS data:  $\bullet$   $\langle u^3 \rangle$ ,  $\blacksquare$   $\langle u^2 v \rangle$ ,  $\blacktriangle$   $\langle uv^2 \rangle$ ,  $\blacktriangledown$   $\langle v^3 \rangle$ , RANS-DNS with error —



**$Re_T = 550$**



**$Re_T = 5200$**

DNS data:  $\bullet$   $\langle u^2 \rangle$ ,  $\blacksquare$   $\langle v^2 \rangle$ ,  $\blacktriangle$   $\langle w^2 \rangle$ ,  $\blacktriangledown$   $\langle uv \rangle$ , RANS-DNS with error —

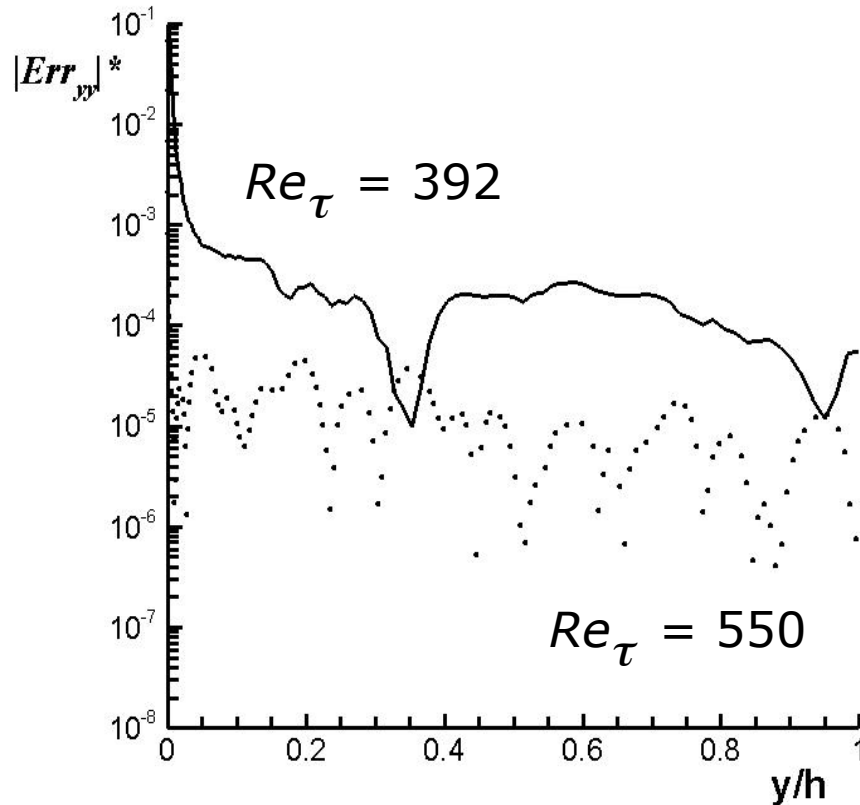
**Uncertainties in DNS data are the current dominant source of uncertainties in RAND-DNS simulations.**

How to deal with sensitivity of RANS equations for the modeling purposes is an open issue, but this sensitivity makes RANS-DNS simulations a convenient tool for the UQ analysis of DNS data.

**S. V. Poroseva, J. D. Colmenares F., S. M. Murman, Physics of Fluids, 2016.**

**S. V. Poroseva, E. Jeyapaul, S. M. Murman, J. D. Colmenares F. AIAA2016-3940**

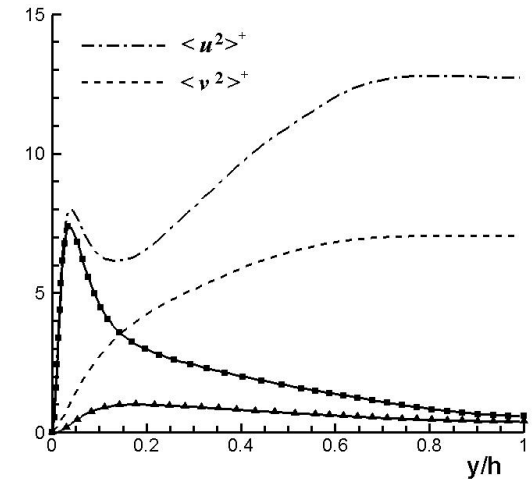
# Uncertainty in DNS data (balance errors)



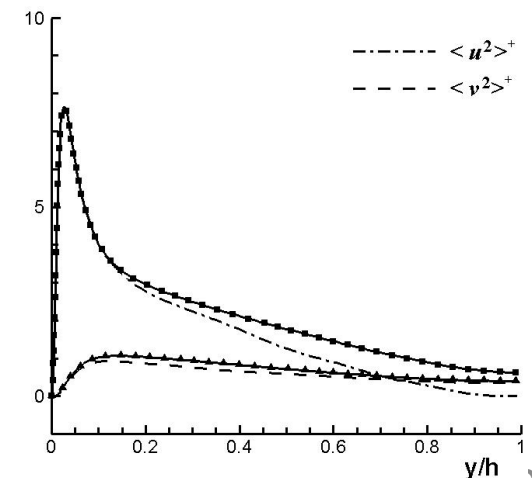
$$|Err_{yy}|^* = |Err_{yy}| / \langle v^2 \rangle$$

Balance errors < 0.1% of  $\langle u_i u_j \rangle$

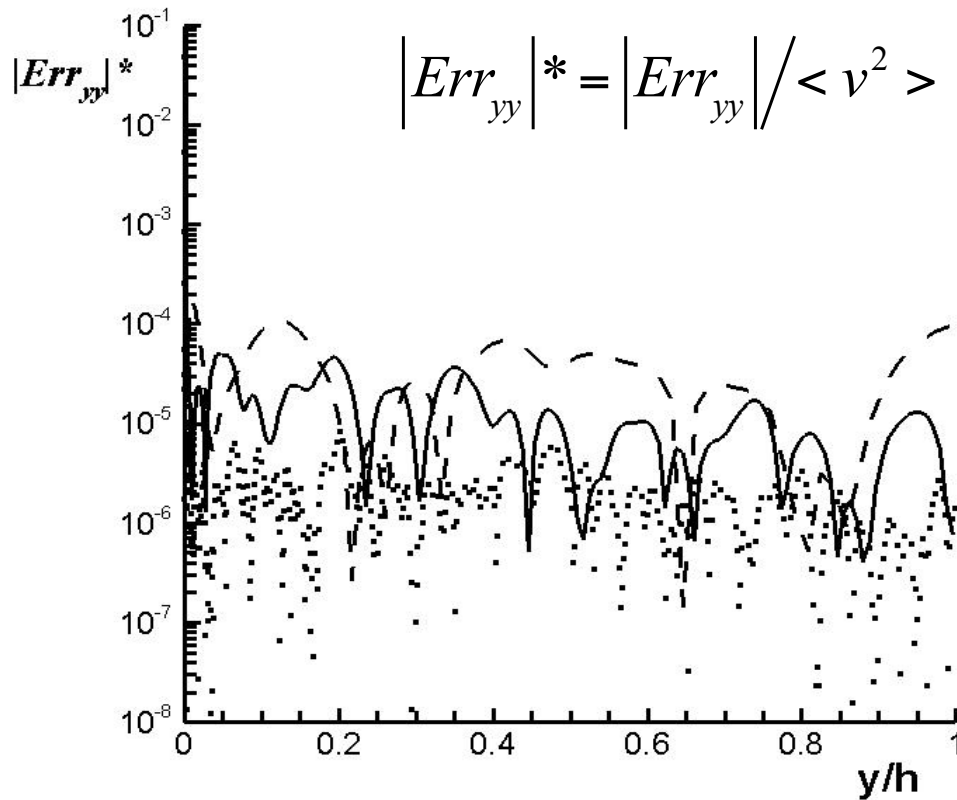
Jeyapaul et al., 2015  $Re_\tau = 392$



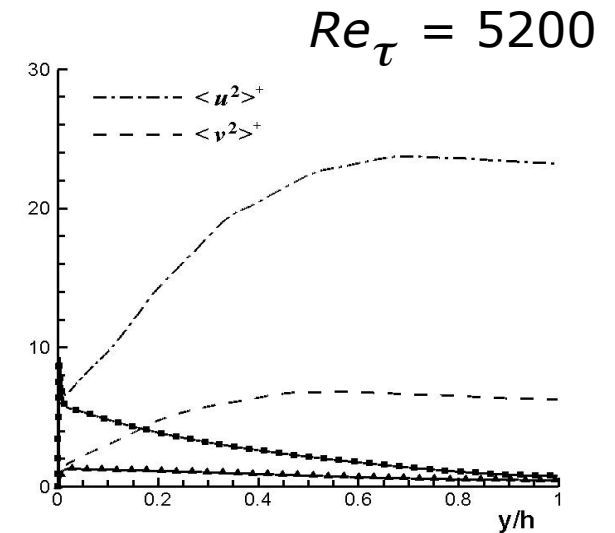
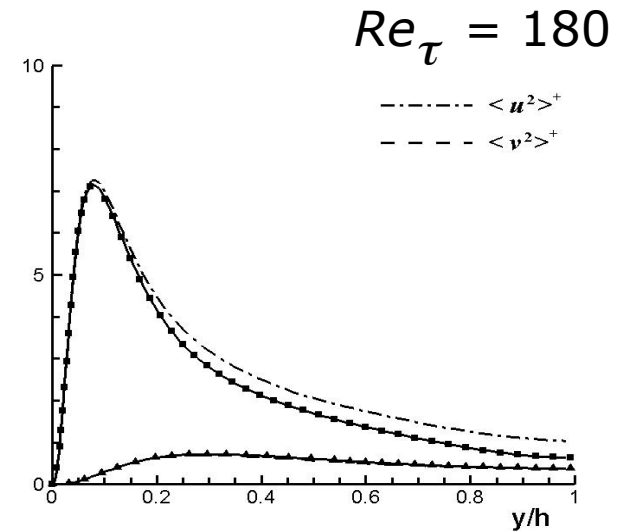
Lee & Moser, 2015  $Re_\tau = 550$



# Balance errors at different Re

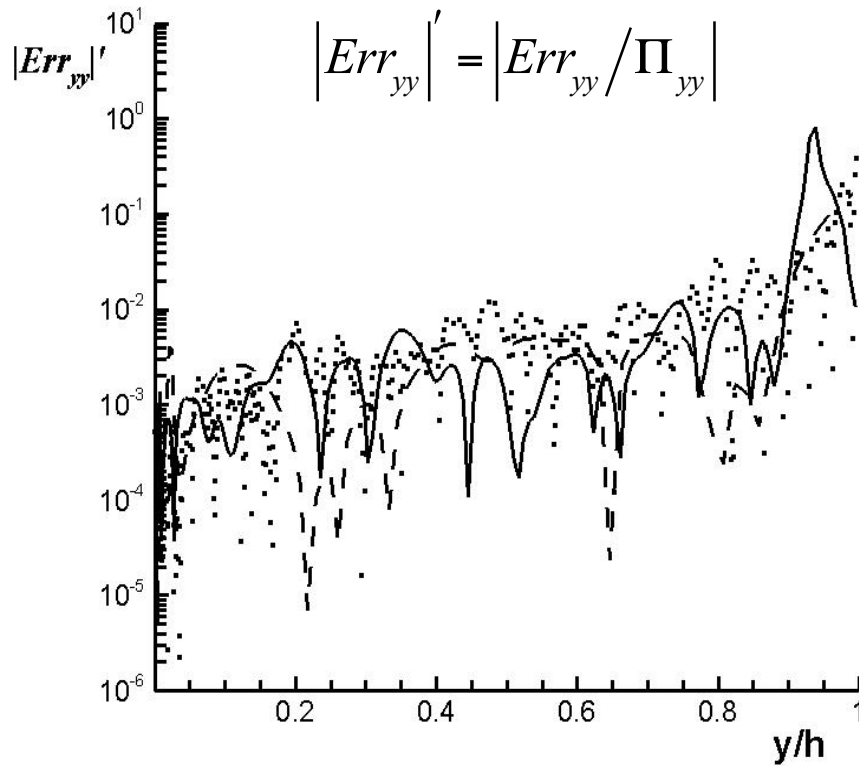


$Re_\tau = 5200$  .....  
 $Re_\tau = 550$  ———  
 $Re_\tau = 180$  - - -



# (Contd.)

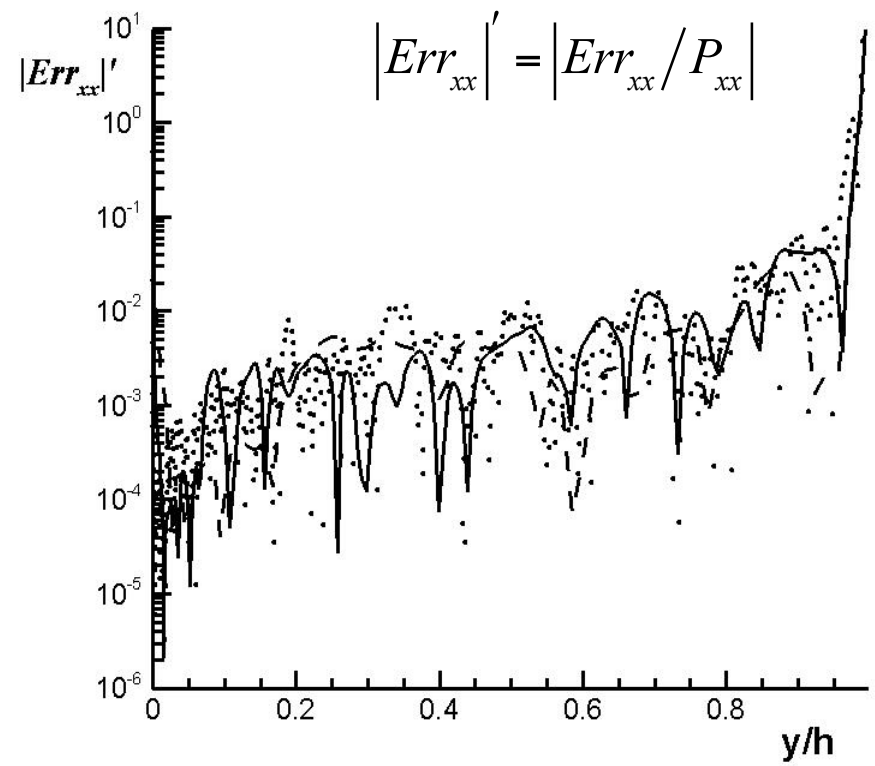
Lee & Moser, 2015



$Re_\tau = 5200$     .....   

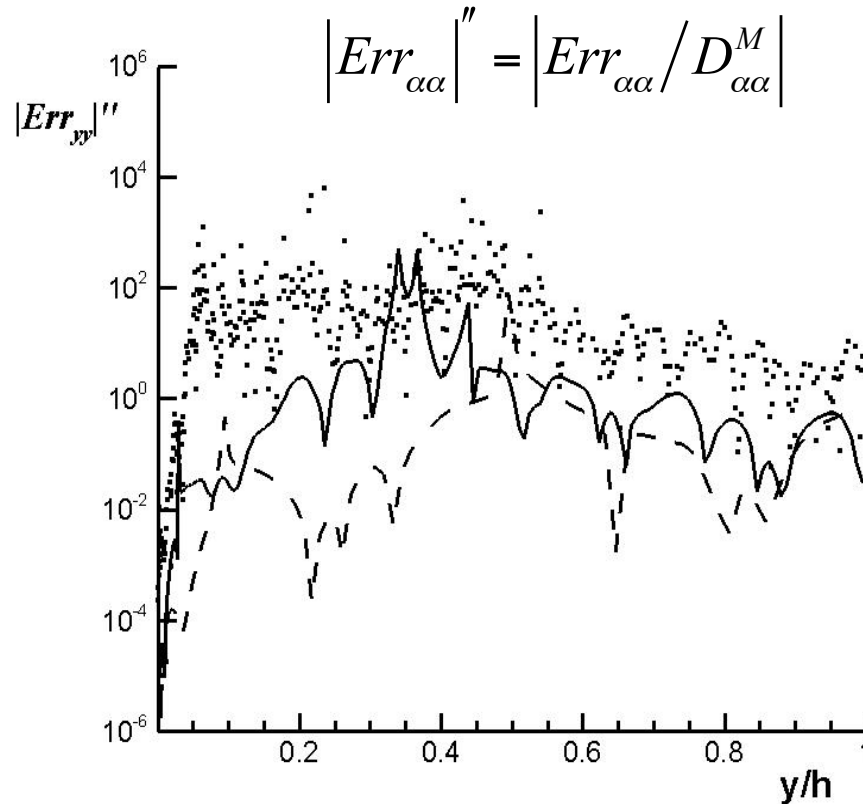
$Re_\tau = 550$     ———   

$Re_\tau = 180$     - - -   



Balance errors < 1% in such normalization with these data

# Balance errors vs. viscous diffusion

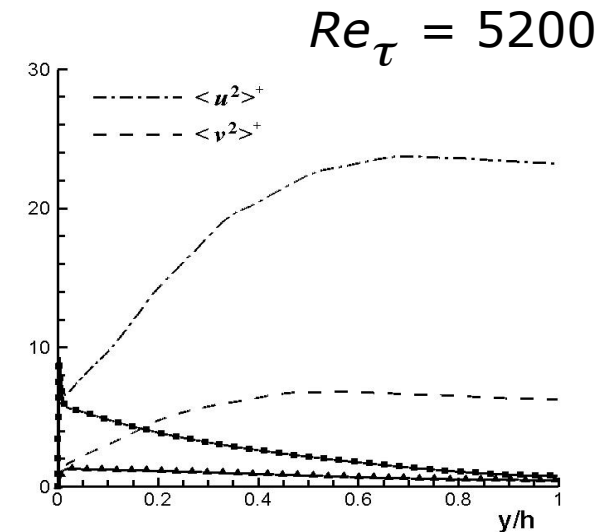
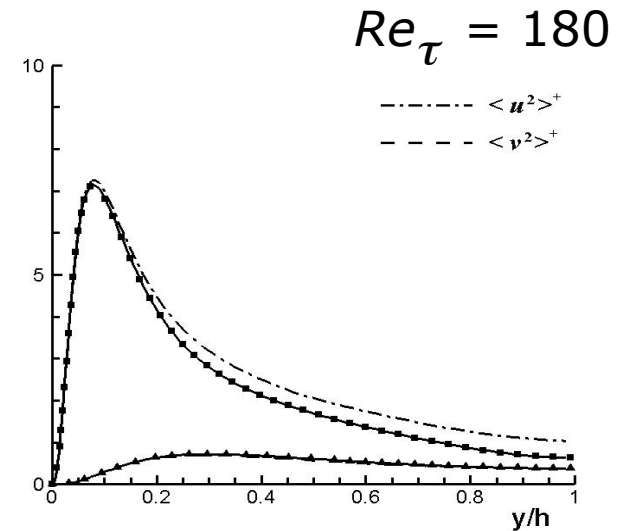


$Re_{\tau} = 5200$  .....

$Re_{\tau} = 550$  ———

$Re_{\tau} = 180$  - - -

Balance errors are huge....



# UQ metric for quantitative analysis

$$\Delta_{\max} = \frac{|g(y) - f(y)|_{\infty}}{|g(y)|_{\infty}} \quad \text{based on } L_{\infty}\text{-norm}$$

$g(y)$  – DNS profile

$f(y)$  – RANS-DNS solution

Lee & Moser, 2015 (in %)

$\Delta_{\max}$	$\langle u^2 \rangle$	$\langle v^2 \rangle$	$\langle uv \rangle$	$\langle w^2 \rangle$
$Re_{\tau} = 180$	6	5	5	13
$Re_{\tau} = 550$	10	17	21	20
$Re_{\tau} = 5200$	287	548	173	308



# (Contd.)

in %

Lee &  
Moser, 2015  
Jeyapaul et  
al., 2015

$\Delta_{\max}$	$\langle u^2 \rangle$	$\langle v^2 \rangle$	$\langle uv \rangle$	$\langle w^2 \rangle$
$Re_{\tau} = 550$	10	17	21	20
$Re_{\tau} = 392$	164	663	629	507

Jeyapaul et  
al., 2015

	$\langle u^2 \rangle$	$\langle v^2 \rangle$	$\langle uv \rangle$	$\langle w^2 \rangle$
$\Delta_{\max}$	164	663	629	507
	$\langle u^3 \rangle$	$\langle v^3 \rangle$	$\langle uv^2 \rangle$	$\langle u^2v \rangle$
$\Delta_{\max}$	625	1290	1170	243
	$\langle u^4 \rangle$	$\langle v^4 \rangle$	$\langle uv^3 \rangle$	$\langle u^3v \rangle$
$\Delta_{\max}$	125	1970	474	354

# Contribution of the statistical error

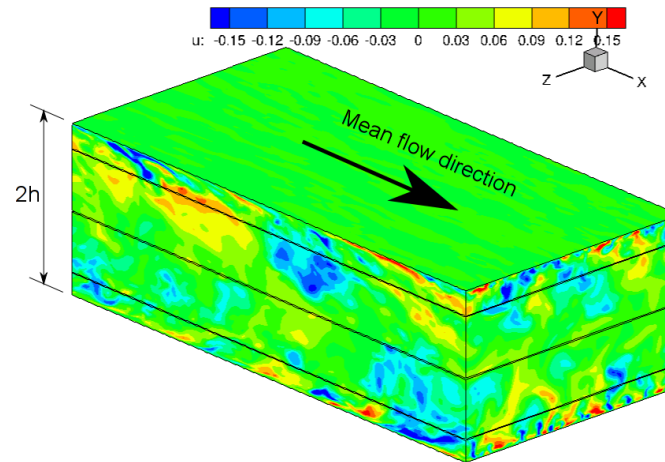
Poroseva et al., AIAA2016-3940

Test case: channel flow  $Re_\tau = 392$

DNS pseudo-spectral (Fourier/Chebyshev- $\tau$ ) method

Coleman et al. 2003

$2\pi h \times 2h \times \pi h$



256x193x192  
spectral modes

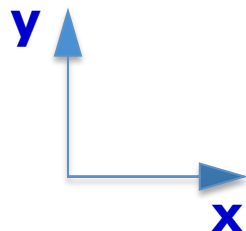
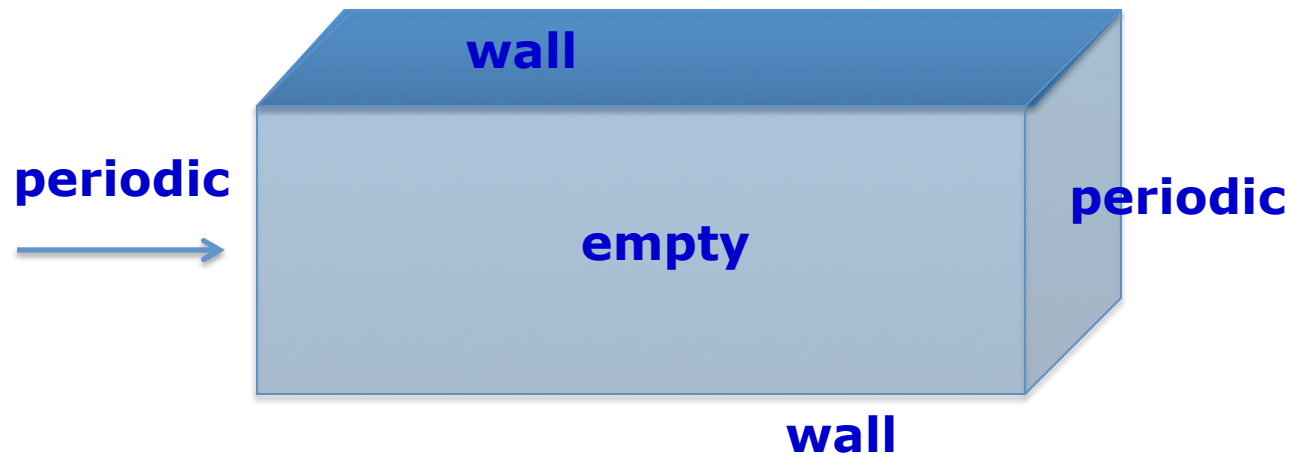
N	1	2	3	4	5	6	7
realizations	25	50	100	159	200	500	1000
t steps	4.72 $\times 10^6$	5.01 $\times 10^6$	5.51 $\times 10^6$	6.1 $\times 10^6$	6.51 $\times 10^6$	9.51 $\times 10^6$	14.69 $\times 10^6$

# RANS-DNS simulations

$$Re_{\tau} = 392$$

$$0 = D_{ij}^M + D_{ij}^T + P_{ij} + \Pi_{ij} - \varepsilon_{ij}$$

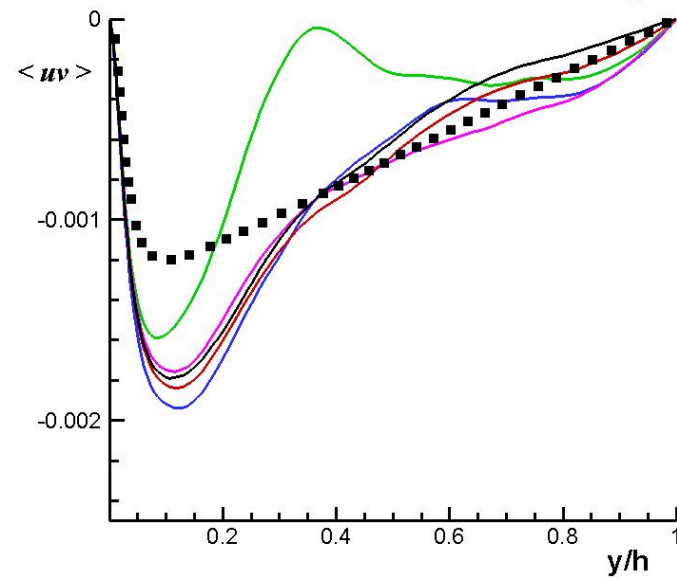
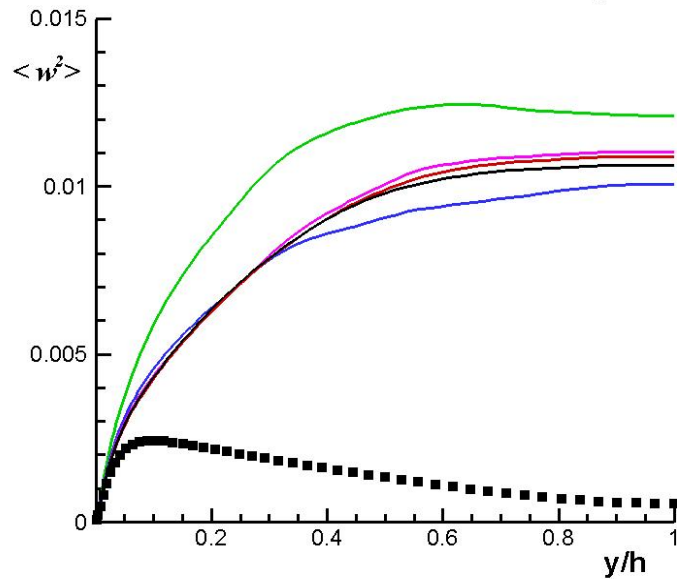
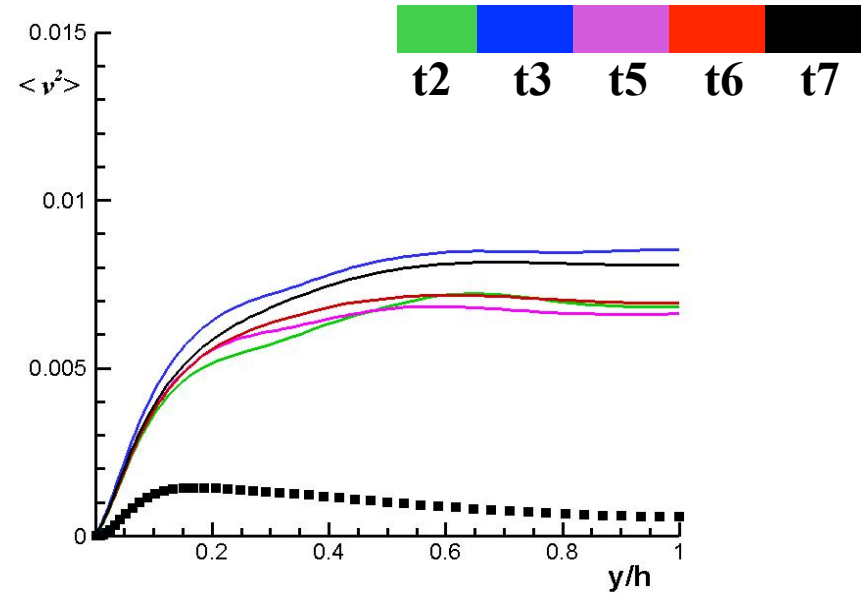
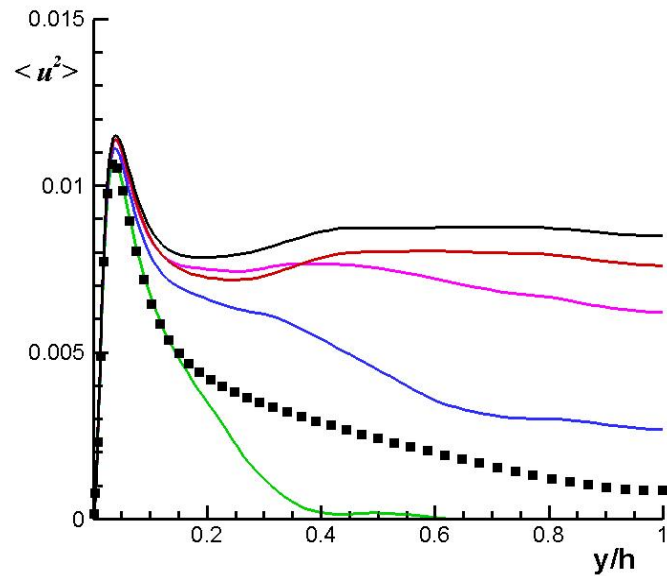
Solver: OpenFOAM



$$L_x \times L_y \times L_z = 0.1h \times 2h \times 0.1h$$

$$N_x \times N_y \times N_z = 2 \times 193 \times 2$$

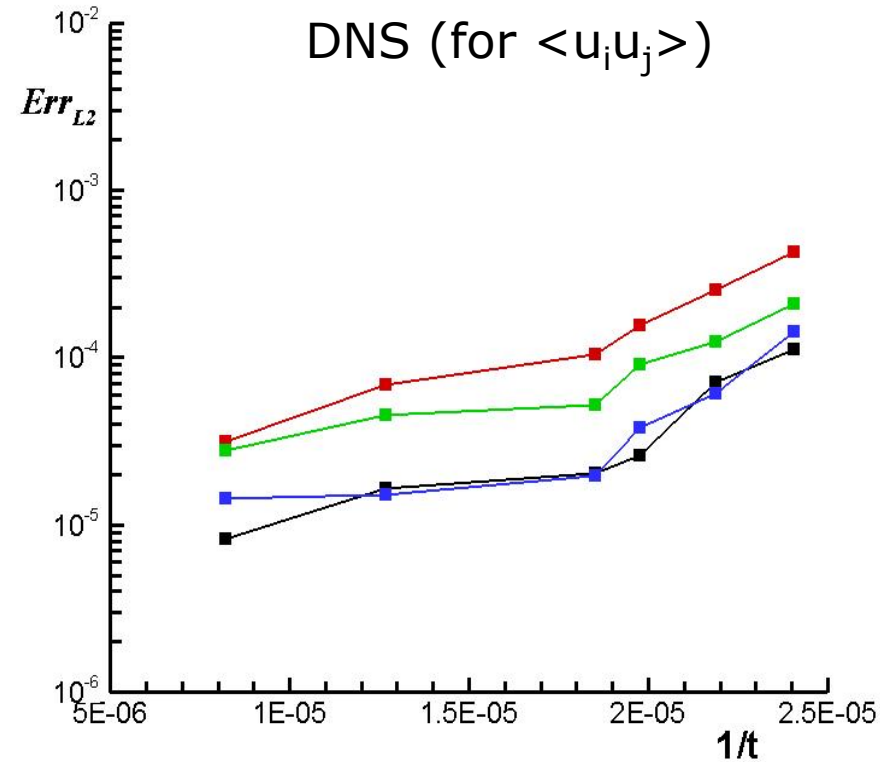
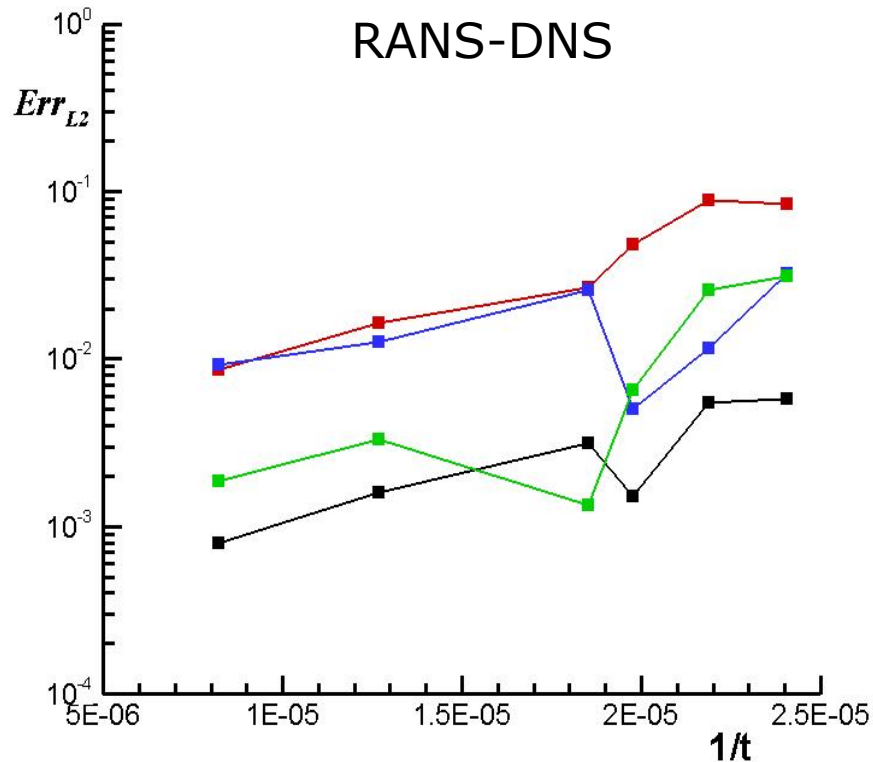
# RANS-DNS convergence



# Error convergence

$$Err_{L2} = ||f(t_n) - f(t_7)||$$

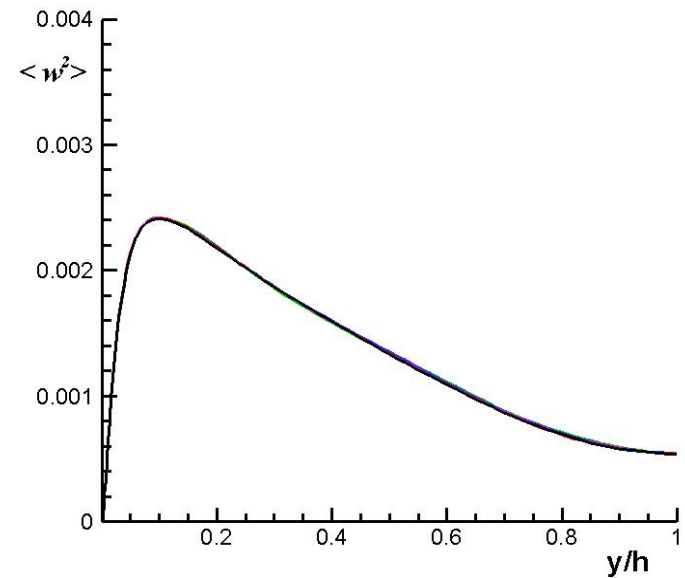
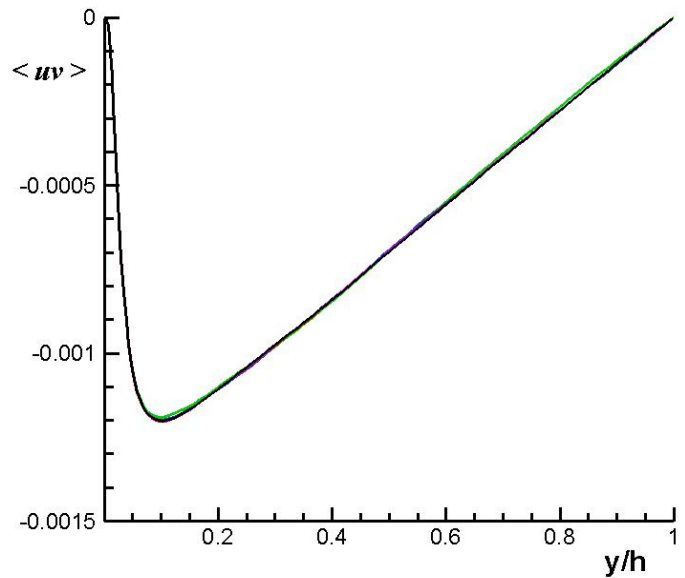
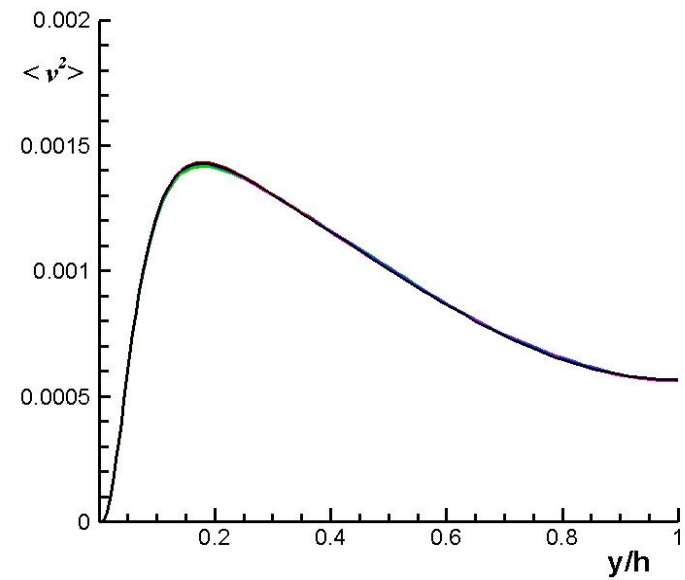
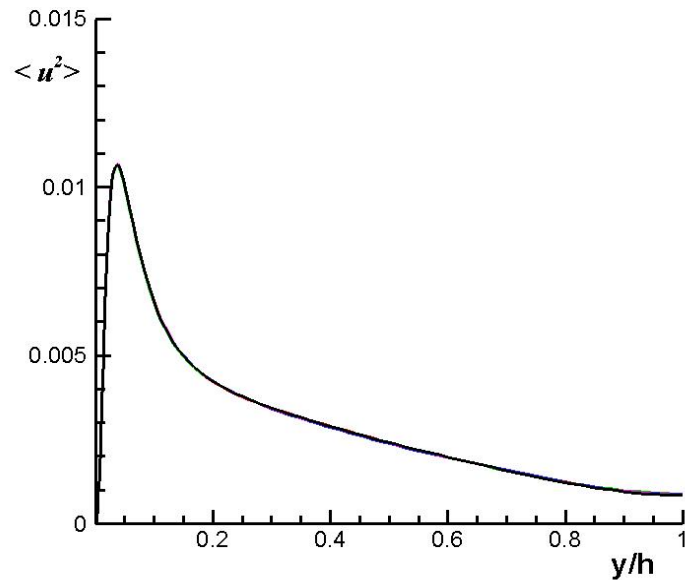
■  $\langle w^2 \rangle$ 
■  $\langle v^2 \rangle$ 
■  $\langle u^2 \rangle$ 
■  $\langle uv \rangle$



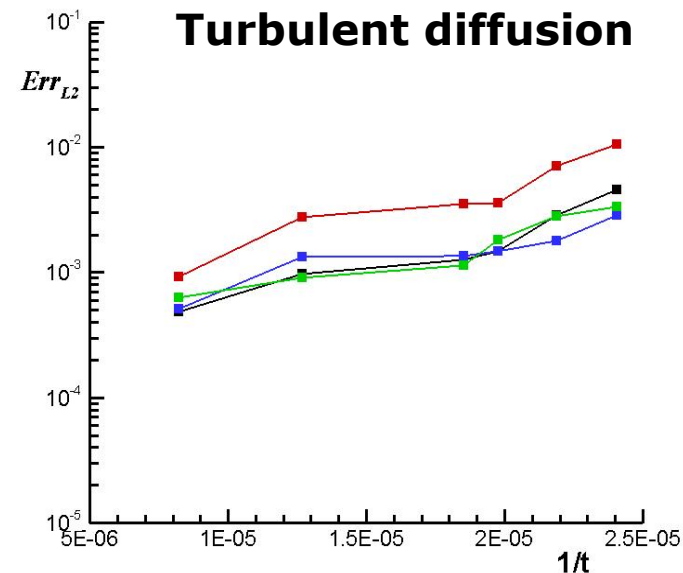
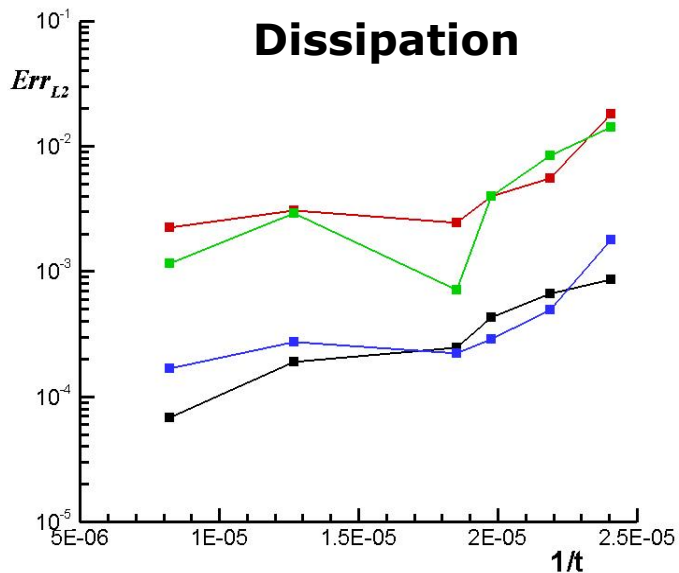
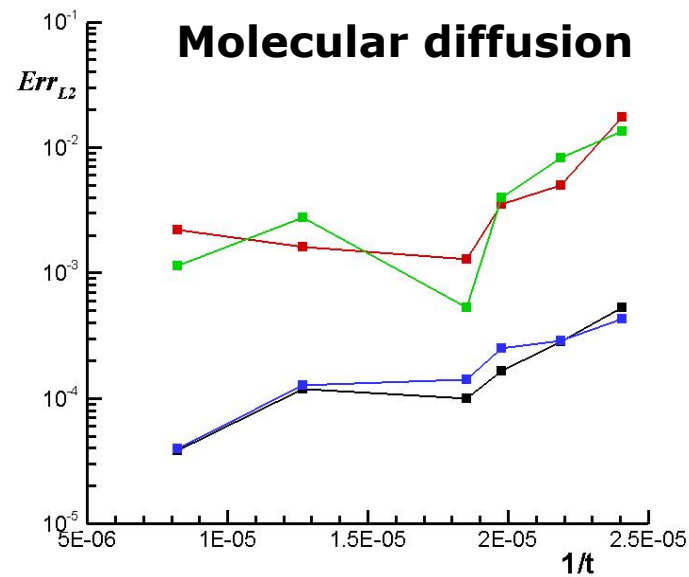
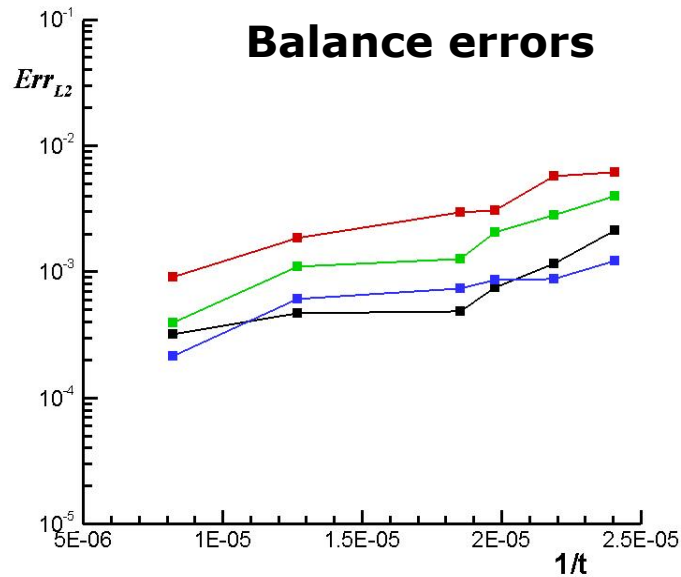
There is a systematic error in DNS and RANS-DNS data

The systematic error is not obvious when the DNS profiles are plotted, instead of their errors (next slide).

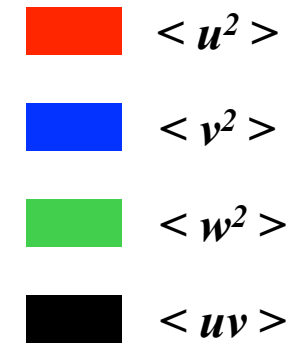
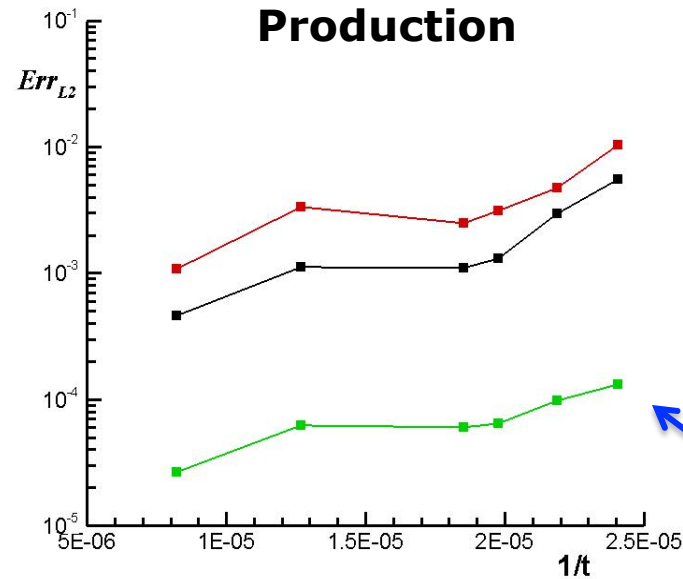
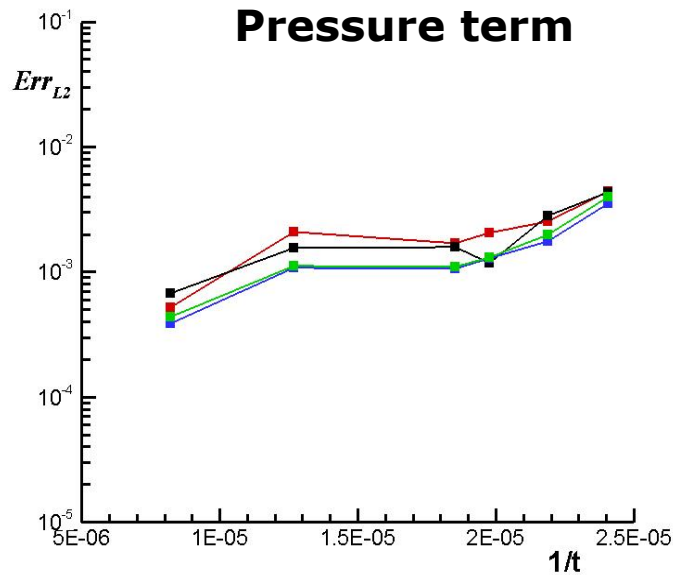
# DNS data convergence



# Error convergence for terms in the DNS budgets



# (Contd.)



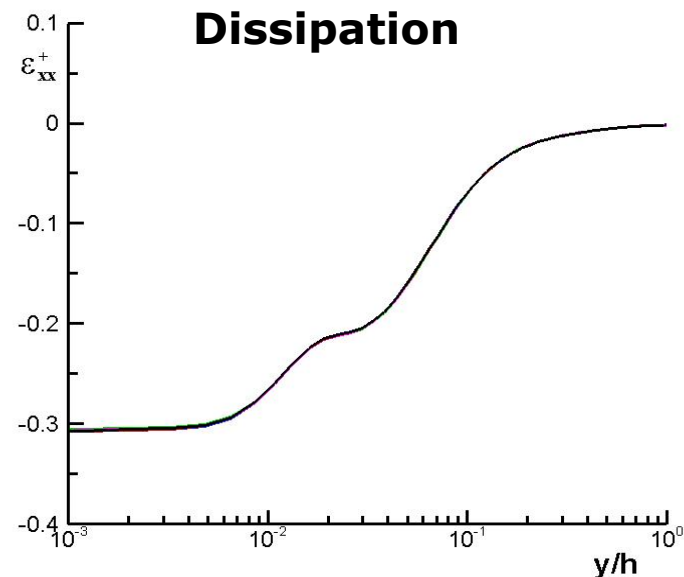
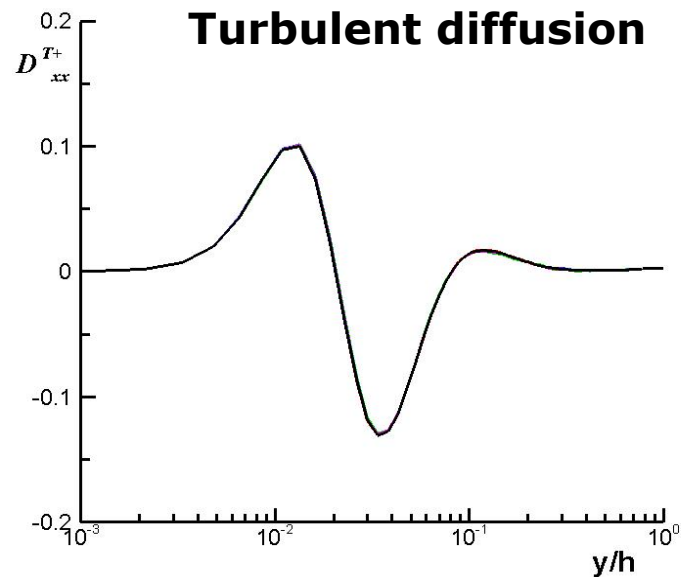
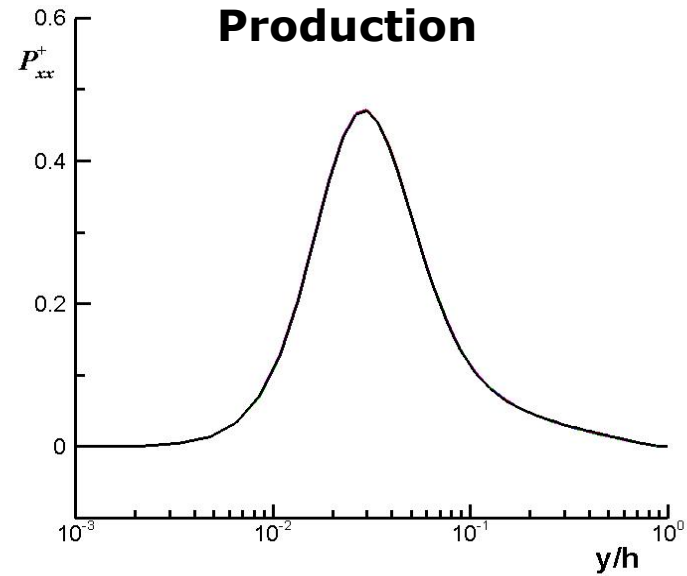
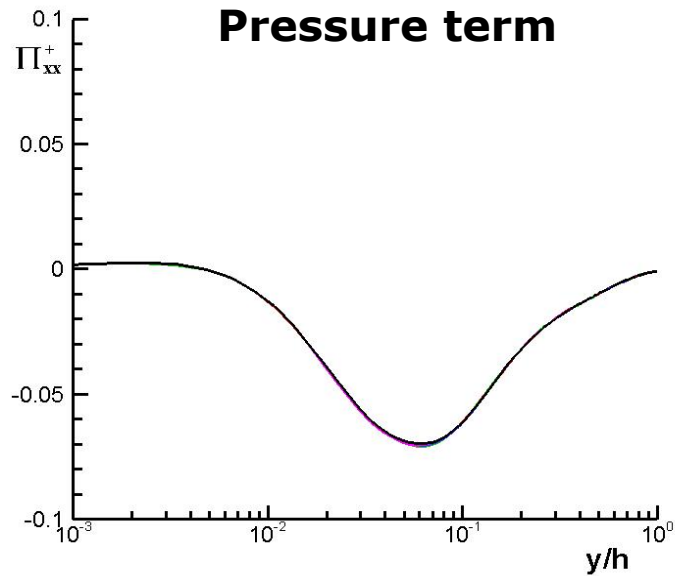
“zero” term

None of the terms converges in statistical sense.

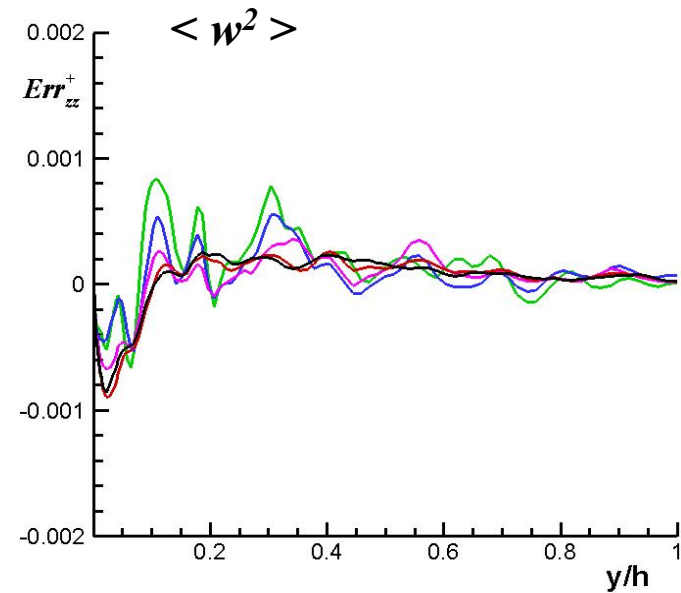
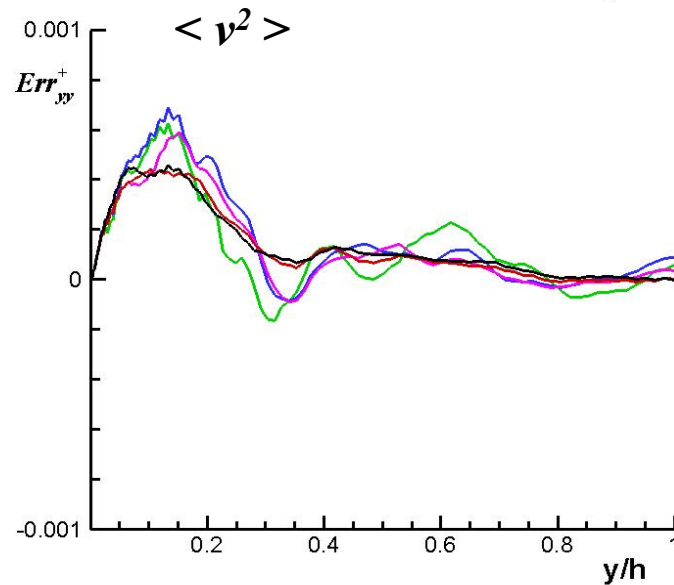
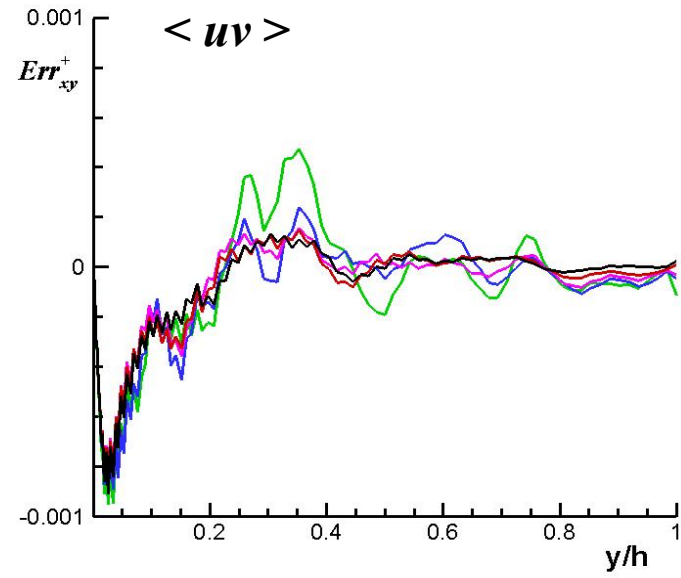
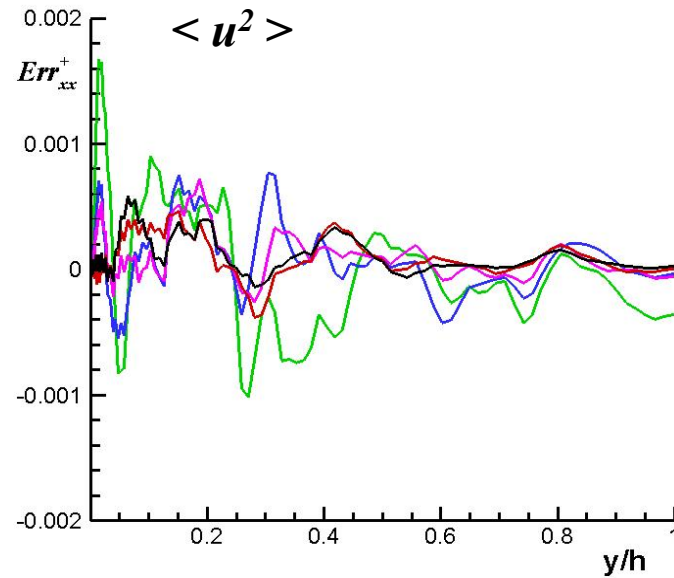
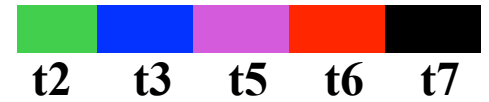
The systematic error is not obvious when their DNS profiles are plotted, instead of their errors (next slide).



# Convergence of $\langle u^2 \rangle$ -budget terms



# Balance error convergence



# Summary

- The current balance errors are too high to compare with the molecular diffusion terms in all considered datasets except for very small Reynolds numbers. **This is a concern when using DNS data for model validation and model development (data-driven approaches) particularly near walls.**
- RANS-DNS simulations are rigorous, easy-to-implement framework for UQ in DNS data.
- DNS data (Reynolds stresses and terms in their budgets) do not converge in the statistical sense. **Running DNS longer does not seem to eliminate the systematic error present in the data.** The study has to be conducted with other solvers.
- The specific origin of the systematic error is currently unknown, but balance errors have a non-uniform distribution in the wall-normal direction, which may indicate an issue with the grid resolution.

# Current

**Test cases:** mixing layer, channel flow **Solver:** Nek5000

in collaboration with Dr. Y. Peet (ASU)

## NASA interests?

Compressible flow DNS, modeling, experiments

# Acknowledgements

J. D. Colmenares F. (Ph.D. student at UNM)

Dr. G. Coleman (NASA Langley)

Dr. E. Jeyapaul (NASA Langley; GE, India)

AIAA TMBWG

## **My current visit to NASA Ames:**

Dr. M. Rogers

Dr. C. Kiris

Dr. M. Olsen

# Questions?

<http://www.unm.edu/~poroseva/>